

See discussions, stats, and author profiles for this publication at: <https://www.researchgate.net/publication/337184803>

Minimizing Production Operation Cycle Time Using Exponential Distribution Heuristic

Article in *Journal of Mechanical Engineering* · November 2018

CITATIONS

0

READS

50

6 authors, including:



Muthuraman R.K.

Periyar Maniammai University

4 PUBLICATIONS 0 CITATIONS

[SEE PROFILE](#)



Ajith Arul Daniel

Vels University

17 PUBLICATIONS 76 CITATIONS

[SEE PROFILE](#)



Vijayananth Suyamburajan

Vels University

22 PUBLICATIONS 3 CITATIONS

[SEE PROFILE](#)

Some of the authors of this publication are also working on these related projects:



Superplastic forming [View project](#)



CFD analysis [View project](#)



MINIMIZING PRODUCTION OPERATION CYCLE TIME USING EXPONENTIAL DISTRIBUTION HEURISTIC

R. Pugazhenth

Associate Professor, Department of Mechanical Engineering,
Vels Institute of Science, Technology and Advanced Studies, Tamilnadu, India.

R K Muthuraman

Assistant professor, Department of Aerospace Engineering,
Periyar Maniammai University, Thanjavur, Tamil Nadu, India

S. Ajith Arul Daniel

Assistant Professor, Department of Mechanical Engineering,
Vels Institute of Science, Technology and Advanced Studies, Tamilnadu, India.

S.Vijayananth

Associate Professor, Department of Mechanical Engineering,
Vels Institute of Science, Technology and Advanced Studies, Tamilnadu, India.

ABSTRACT

In any production flowshop, the total completion time should be optimal as possible. Many algorithms had done on this work. For identifying an optimum sequence for 'n' jobs in 'm' machines, $n!$ Sequences to be worked. Since limitation in computing capabilities, the heuristics are required to evaluate an optimal sequence in an easy way. The classical algorithm like RA, Palmer, CDS methods gives the near to optimal makespan time. But the optimum results couldn't be obtained so far. This paper deals with the heuristic to get an optimal sequence in a flowshop. An algorithm is newly proposed based on exponential function from mathematical and computational aspects to identify the optimal sequence. Using the taillard flowshop problem, the proposed heuristic was compared with an existing heuristic. As an outcome, well-bound results are obtained which are better as compared. The degree of elapse time to lower bound are evaluated and graphically presented.

Keywords: Flow shop, Makespan, Exponential distribution, MATLAB, Optimization.

Cite this Article: R. Pugazhenth, R K Muthuraman, S. Ajith Arul Daniel and S.Vijayananth, Minimizing Production Operation Cycle Time Using Exponential Distribution Heuristic, International Journal of Mechanical Engineering and Technology, 9(11), 2018, pp. 1429–1437.

<http://www.iaeme.com/IJMET/issues.asp?JType=IJMET&VType=9&IType=11>

1. INTRODUCTION

Many algorithms and heuristics had been developed so far. All these methodologies are directly to identify an optimum makespan. Since the makespan is reduced; idle time of the machines, the waiting time of the jobs and other parameters also controlled indirectly. A scheduling problem is to find a minimum total completion time giving a sequence of 'n' jobs on given 'm' machines, to address different kinds of production oriented problems in manufacturing and genetic industries. In 1954, a simple algorithm was given by Johnson [1], for flowshop scheduling problems for 'n' jobs in 2 machines. This work was further developed by Ignall and Schrage [2], Bagga. (1969), Szwarc (1977), Anup (2002), Singh (2005), Gupta (2006).

2. LITERATURE REVIEW

The production of finished products from raw materials needs several operations to be performed in a given sequence. Frequently, similar operations required for several products are performed at the same workstation, particularly when the products are produced on a mass scale; it is required to select a preferred order for products passing through a work center. The problem becomes complex when there are several workstations serving many products. In all such problems, the criterion of selection is minimum total processing time. Sharma et al [3] studied for 'n' jobs in 2 machines in flowshop problem to minimize rental cost under the predefined rental policy in which probabilities have been associated with processing time including breakdown interval and job – block criteria. The study made by Gupta et al [4] by introducing the concept of set up time separated from processing time, each associated with probabilities including job block criteria and breakdown interval.

The flowshop scheduling problem has been a keen area for the researchers over five decades. It is generally not practicable to solve such problems by enumeration. Unfortunately, generalized sequencing models are also not available to deal with all cases. The solution method in such cases was first developed by Johnson. The NP-completeness of the flowshop-scheduling problem was discussed widely by Quan-Ke Pan and Ling Wang [5]. In the 1965's Palmer [6] have been the first to propose heuristic procedures. The first significant work in the development of an efficient heuristic is due to Campell, Dudek, and Smith [7]. Their algorithm consists essentially in splitting the given m-machine problem into a series of an equivalent two-machine flow shop problem and solving by Johnson's rule. In 1977, Dannenbring [8] has developed a procedure called 'rapid access', which attempts to combine the advantages of Palmer's slope index and CDS procedures. Though the procedure by Dannenbring has found to yield better quality solution than those by Palmer's and CDS methods; it requires much more computational effort.

During the 1980s, King and Spachis [9] treated the makespan problem as equivalent to that of minimizing total delay and run-out delay. They have proposed heuristics that aim at matching the two consecutive job time-block profiles by considering these delays. One of the heuristics turns out to be better than the CDS heuristic. In 1982, Stinson et al [10] have proposed a radically different approach. They treated the makespan oriented problem as a traveling salesman problem and developed a procedure in two steps. The heuristic solution is found to yield better quality solution than those by Palmer [11] and CDS methods at the cost of increased computational effort. In 1983, Nawaz et al [12] presented a heuristic based on the premise that a job with higher total processing time should be given higher priority than a job with less total processing time. A schedule is developed by the job-insertion technique. The number of enumeration's in the heuristic method is $\frac{1}{2} n (n+1) - 1$.

A simple modification and extension of Palmer's heuristic were carried out by Hundal and Rajagopal [13]. Two sets of indices have been proposed and three sequences were obtained. In 1989, Widner and Hertz [14] proposed a new heuristic called Sequencing Problem involving a Resolution by Integrated Taboo search technique (SPIRIT). Osman and Potts [15] and Ogbu and

Smith [16] made use of simulated annealing; a heuristic technique adapted to a number of combinatorial optimization problems. Simulated annealing follows the same basic steps which are used in the conventional descent method. In 2013, Pugazhenthil and Anthony Xavier [16] reported a dummy machine concept with the advancement of Pascal's triangle method (PTM), followed by Johnson's algorithm. The advance of this work had been proposed by Pugazhenthil and Anthony Xavier [17] as a current view. This new work is a methodology using an exponential function from mathematical and computational aspects to overcome the results of the above-mentioned algorithms and the results are represented graphically. For the general comparison, the Taillard [18] had proposed a set of flowshop problems for 20, 50 and 100 jobs on 5, 10 and 20 machines are considered.

3. METHODOLOGY

3.1. EXPONENTIAL EVALUATION

This algorithm distributes a factor to the processing time of the jobs in each machine from the advancement of the classical algorithm. This factor added to the job is evaluated through the exponential equation, which gives a value of the index to the respective job. By sorting the index value, the optimal order of sequence can be obtained. From the illustration of Palmer, the Palmer sequence can provide an optimum elapsed time. The advancement of his methodology is proposed as a new heuristic to evaluate the optimal elapsed time. This heuristic provides 'n' values which are to be descended and respective jobs to be sequenced. Using the Taillard benchmark flowshop problem, the newly proposed heuristic is compared with the proposed algorithm. The processing times vary from 1 to 99-time units and they are generated using a random number generator for different seeds.

3.2. PROCEDURE FOR NEWLY PROPOSED HEURISTIC

Step 1: Let 'n' number of jobs to be machined on 'm' machines. It is assumed that all jobs are present for processing at time zero. And one job can run in one machine at a time without changing the machine order.

Step 2: The exponential index to be calculated using the exponential equation for n jobs.

$$y_j = \sum_{i=0}^{m-1} (2.61 * m - \exp(i)) * T_{m-i}$$

Where, Y_j = exponential index value for j^{th} job,

m = number of machines

$T_{(m-i)}$ = process time of job under $(m-i)^{\text{th}}$ machine

Step 3: sort the exponential index in descending order.

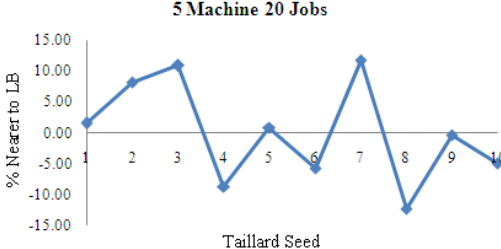
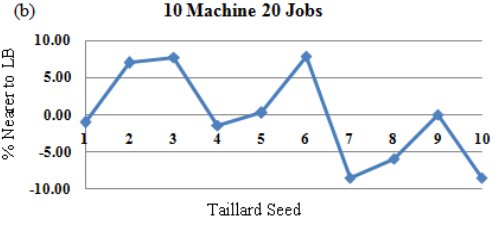
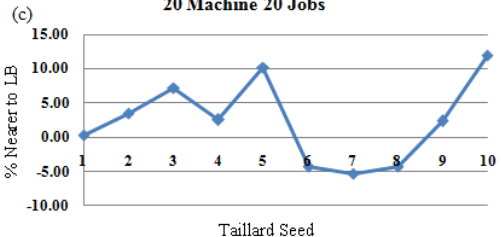
Step 4: based on the sorted value, the jobs to be sequenced.

4. ANALYSIS OF NEW HEURISTIC OVER A PROPOSED HEURISTIC

Using the above-mentioned algorithm, the set of results are obtained in MATLAB programming environment. From the table 1, the results are compared and examined to the lower bound values of Taillard flowshop problem. From these results, the graphical representations (Figure 1(a) - 1(i)) are done.

The degree of optimal for newly proposed heuristic over a proposed heuristic is obtained from each set of seed; which is shown in table 2 and it has been graphically denoted in figure 2.

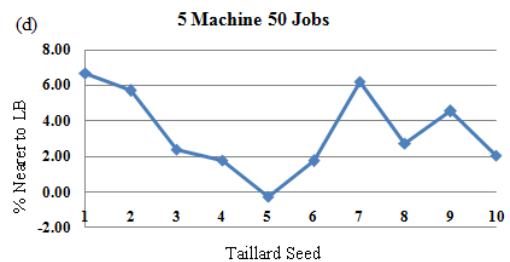
Table 1 Statistic of new heuristic over a proposed heuristic

| 5 m 20 jobs | | | | |  |
|----------------|-------------|--------------------|------|--------------|--|
| Taillard Seeds | Lower Bound | Proposed Heuristic | PTM | Near to LB % | |
| 873654221 | 1232 | 1377 | 1398 | 1.50 | |
| 379008056 | 1290 | 1360 | 1481 | 8.17 | |
| 1866992158 | 1073 | 1236 | 1387 | 10.89 | |
| 216771124 | 1268 | 1564 | 1438 | -8.76 | |
| 495070989 | 1198 | 1342 | 1354 | 0.89 | |
| 402959317 | 1180 | 1385 | 1310 | -5.73 | |
| 1369363414 | 1226 | 1268 | 1438 | 11.82 | |
| 2021925980 | 1170 | 1504 | 1339 | -12.32 | |
| 573109518 | 1206 | 1434 | 1428 | -0.42 | |
| 88325120 | 1082 | 1298 | 1237 | -4.93 | |
| 10 m 20 jobs | | | | |  |
| Taillard Seeds | Lower Bound | Proposed Heuristic | PTM | Near to LB % | |
| 587595453 | 1448 | 1915 | 1896 | -1.00 | |
| 1401007982 | 1479 | 1928 | 2073 | 6.99 | |
| 873136276 | 1407 | 1737 | 1883 | 7.75 | |
| 268827376 | 1308 | 1727 | 1703 | -1.41 | |
| 1634173168 | 1325 | 1713 | 1718 | 0.29 | |
| 691823909 | 1290 | 1618 | 1757 | 7.91 | |
| 73807235 | 1388 | 1870 | 1725 | -8.41 | |
| 1273398721 | 1363 | 1928 | 1821 | -5.88 | |
| 2065119309 | 1472 | 1832 | 1832 | 0.00 | |
| 1672900551 | 1356 | 2035 | 1876 | -8.48 | |
| 20 m 20 jobs | | | | |  |
| Taillard Seeds | Lower Bound | Proposed Heuristic | PTM | Near to LB % | |
| 479340445 | 1911 | 2606 | 2614 | 0.31 | |
| 268827376 | 1711 | 2516 | 2608 | 3.53 | |
| 1958948863 | 1844 | 2575 | 2776 | 7.24 | |

| | | | | |
|----------------|------|------|------|-------|
| 918272953 | 1810 | 2561 | 2628 | 2.55 |
| 555010963 | 1899 | 2513 | 2799 | 10.22 |
| 201085149 1 | 1875 | 2697 | 2588 | -4.21 |
| 151983330 3 | 1875 | 2687 | 2551 | -5.33 |
| 174867093 1 | 1880 | 2676 | 2568 | -4.21 |
| 192349758 6 | 1840 | 2553 | 2615 | 2.37 |
| 182990996 7 | 1900 | 2372 | 2695 | 11.99 |

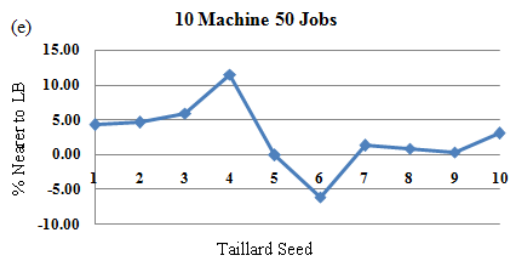
5M 50J

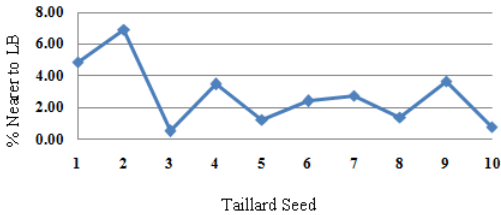
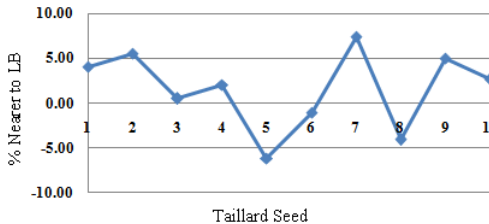
| Taillard Seeds | Lower Bound | Proposed Heuristic | PTM | Near to LB % |
|----------------|-------------|--------------------|------|--------------|
| 1328042058 | 2712 | 2906 | 3114 | 6.68 |
| 200382020 | 2808 | 3055 | 3240 | 5.71 |
| 496319842 | 2596 | 2902 | 2974 | 2.42 |
| 1203030903 | 2740 | 3052 | 3108 | 1.80 |
| 1730708564 | 2837 | 3125 | 3117 | -0.26 |
| 450926852 | 2793 | 3067 | 3122 | 1.76 |
| 1303135678 | 2689 | 2858 | 3048 | 6.23 |
| 1273398721 | 2667 | 2984 | 3068 | 2.74 |
| 587288402 | 2527 | 2830 | 2965 | 4.55 |
| 248421594 | 2776 | 2970 | 3033 | 2.08 |



10M 50J

| Taillard Seeds | Lower Bound | Proposed Heuristic | PTM | Near to LB % |
|----------------|-------------|--------------------|------|--------------|
| 1958948863 | 2907 | 3717 | 3883 | 4.28 |
| 575633267 | 2821 | 3429 | 3594 | 4.59 |
| 655816003 | 2801 | 3402 | 3614 | 5.87 |
| 1977864101 | 2968 | 3325 | 3755 | 11.45 |
| 93805469 | 2908 | 3726 | 3723 | -0.08 |
| 1803345551 | 2941 | 3846 | 3625 | -6.10 |
| 49612559 | 3062 | 3624 | 3672 | 1.31 |
| 1899802599 | 2959 | 3640 | 3674 | 0.93 |



| | | | | | |
|----------------|-------------|--------------------|------|--------------|---|
| 2013025619 | 2795 | 3662 | 3675 | 0.35 | <div>(f) 20 Machine 50 Jobs</div>  |
| 578962478 | 3046 | 3655 | 3770 | 3.05 | |
| 20M 50J | | | | | |
| Taillard Seeds | Lower Bound | Proposed Heuristic | PTM | Near to LB % | |
| 1539989115 | 3480 | 4610 | 4846 | 4.87 | |
| 691823909 | 3424 | 4338 | 4661 | 6.93 | |
| 655816003 | 3351 | 4513 | 4537 | 0.53 | |
| 1315102446 | 3336 | 4557 | 4721 | 3.47 | |
| 1949668355 | 3313 | 4603 | 4661 | 1.24 | |
| 1923497586 | 3460 | 4478 | 4589 | 2.42 | |
| 1805594913 | 3427 | 4642 | 4773 | 2.74 | |
| 1861070898 | 3383 | 4534 | 4597 | 1.37 | |
| 715643788 | 3457 | 4417 | 4584 | 3.64 | |
| 464843328 | 3438 | 4646 | 4682 | 0.77 | |
| 5 m 100 jobs | | | | | |
| Taillard Seeds | Lower Bound | Proposed Heuristic | PTM | Near to LB % | <div>(g) 5Machine 100 Jobs</div>  |
| 896678084 | 5437 | 5838 | 6086 | 4.07 | |
| 1179439976 | 5208 | 5536 | 5861 | 5.55 | |
| 1122278347 | 5130 | 5674 | 5702 | 0.49 | |
| 416756875 | 4963 | 5425 | 5540 | 2.08 | |
| 267829958 | 5195 | 6165 | 5810 | -6.11 | |
| 1835213917 | 5063 | 5520 | 5463 | -1.04 | |
| 1328833962 | 5198 | 5497 | 5938 | 7.43 | |
| 1418570761 | 5038 | 5754 | 5529 | -4.07 | |
| 161033112 | 5385 | 5738 | 6040 | 5.00 | |
| 304212574 | 5272 | 5587 | 5745 | 2.75 | |
| 10 m 100 jobs | | | | | |
| Taillard Seeds | Lower Bound | Proposed Heuristic | PTM | Near to LB % | |

| | | | | |
|----------------|-------------|--------------------|------|--------------|
| 1539989115 | 5759 | 6339 | 6870 | 7.73 |
| 655816003 | 5345 | 6298 | 6422 | 1.93 |
| 960914243 | 5623 | 6497 | 6752 | 3.78 |
| 1915696806 | 5732 | 6742 | 7010 | 3.82 |
| 2013025619 | 5431 | 6617 | 6531 | -1.32 |
| 1168140026 | 5246 | 6279 | 6336 | 0.90 |
| 1923497586 | 5523 | 6476 | 6599 | 1.86 |
| 167698528 | 5556 | 6279 | 6658 | 5.69 |
| 1528387973 | 5779 | 6524 | 6976 | 6.48 |
| 993794175 | 5830 | 6468 | 6954 | 6.99 |
| 20M 100J | | | | |
| Taillard Seeds | Lower Bound | Proposed Heuristic | PTM | Near to LB % |
| 450926852 | 5851 | 7240 | 7840 | 7.65 |
| 1462772409 | 6099 | 7584 | 7613 | 0.38 |
| 1021685265 | 6099 | 7668 | 7830 | 2.07 |
| 83696007 | 6072 | 7616 | 7694 | 1.01 |
| 508154254 | 6009 | 7590 | 7767 | 2.28 |
| 1861070898 | 6144 | 7430 | 7888 | 5.81 |
| 26482542 | 5991 | 7730 | 7827 | 1.24 |
| 444956424 | 6084 | 7589 | 7919 | 4.17 |
| 2115448041 | 5979 | 7433 | 7864 | 5.48 |
| 118254244 | 6298 | 7769 | 7891 | 1.55 |

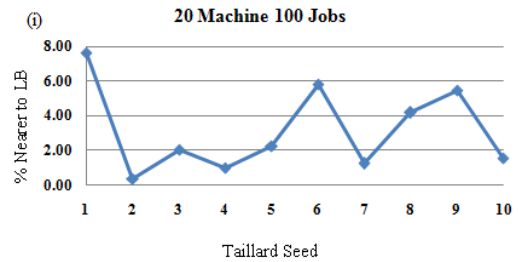
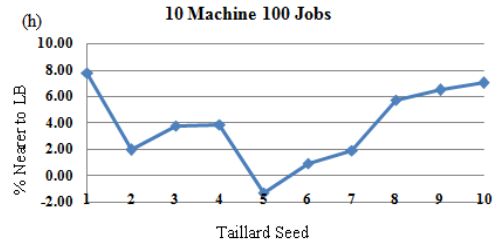


Table 2 Degree of Accuracy

| Machine | Job | Degree of accuracy |
|---------|-----|--------------------|
| 5 | 20 | 1.11 |
| 10 | 20 | -2.22 |
| 20 | 20 | 24.45 |
| 5 | 50 | 33.72 |
| 10 | 50 | 25.64 |
| 20 | 50 | 27.99 |
| 5 | 100 | 16.14 |
| 10 | 100 | 37.87 |
| 20 | 100 | 31.64 |

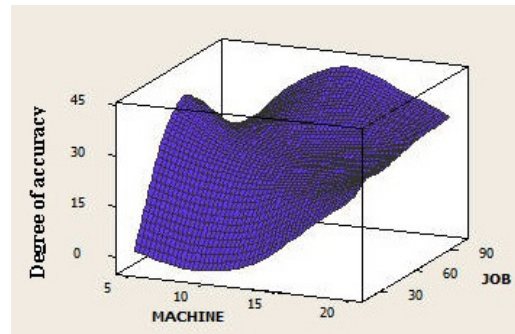


Fig. 2 Degree of Accuracy

The degree of accuracy nearer to lower bound is represented in figure 2. From this figure 2, it concludes that for jobs and machines more, the results are good enough than other proposed heuristic.

5. CONCLUSION

In this research article, a new heuristic is proposed based on exponential distribution function from mathematical and computational criteria to identify the optimal makespan giving sequence in a flow shop. The attempt made was good for a high number of jobs or machine; it was proved by the degree of accuracy chart. The processing times of jobs on machines are taken from Taillard flowshop problem. It noticed that obtained minimum elapsed time for an optimal sequence from the proposed heuristic and it is compared to PTM. The MATLAB program was generated for computational results. These results give a better optimal sequence and which is represented graphically.

REFERENCES

- [1] S.M. Johnson, Optimal two and three machine production scheduling with set up times included, *Nav. Res. Log.*1(1) (1954).
- [2] Ignal, S., Schrage and Lominick, P.: Priority dispatching and job lateness in a job shop. *Journal of Industrial Engineering*, Vol. 6, 228 – 237 (1965).
- [3] Sameer Sharma,Deepak Gupta, Payal Singla, ShashiBala: Minimizing Rental Cost For n-jobs, 2-machines Flow Shop Scheduling, Processing Time Associated With Probabilities Including Transportation Time And Job Block Criteria. *Information and Knowledge Management*. ISSN 2224-5758 (Paper) ISSN 2224-896X(Online) Vol.1, No.3, 2011.
- [4] D.Gupta, S. Sharma and Seema, “Bicriteria in n x 3 flowshop scheduling under specified rental policy, processing time associated with probabilities including transportation time and job block criteria”, *Mathematical Modelling and Theory*. 1(2), 2011, 7-18.
- [5] Quan-Ke Pan and Ling Wang: Effective heuristics for the blocking flowshop scheduling problem with makespan Minimization. *OMEGA*, Vol. 40(2), 218-229 (2012).
- [6] Palmer, D.S.: Sequencing Jobs through a Multi-Stage Process in the Minimum Total Time – A Quick Method of Obtaining a near Optimum. *Operations Research*, Vol.16, 101-107 (1965).
- [7] Dannenbring, D.G.: An Evolution of Flow-Shop Sequencing Heuristics. *Management Science*, Vol. 23, 1174-1182 (1977)
- [8] King, J.R. and Spachis, A.S.: Heuristics for flowshop scheduling. *International Journal of Production Research*, Vol.18 (3), 345-357 (1980)
- [9] Stinson, Simith, D.T. and Hogg, G.L.: A state of art survey of dispatching rules for manufacturing job shop operations. *International Journal of Production Research*, Vol. 20, 27 – 45 (1982).
- [10] Palmer, K.: Sequencing rules and due date assignments in a job shop. *Management Science*, Vol. 30 (9), 1093 – 1104 (1984).
- [11] Nawaz, M., Ensocore, Jr., E and Ham, I.: A Heuristic Algorithm for the m- Machine, n- Job, Flow-shop Sequencing Problem, and OMEGA. *The International Journal of Management Science*, Vol. 11(1), 91-95 (1983).
- [12] Hundal, T.S. and Rajgopal, J.: An extension of Palmer heuristic for the flow-shop scheduling problem. *International Journal of Production Research*, Vol. 26, 1119-1124 (1988).
- [13] Winder, R. and Hertz. A survey of priority based scheduling. *OR. Spectrum*, Vol. 11, 3-16 (1989).
- [14] Osmon, I.H. and Potts, C.N.: A state of art survey of static scheduling research involving due dates. *Omega*, Vol. 12, 63 – 76 (1989).

- [15] Ogbu, F.A. and Smith, D.K.: Simulated annealing for the permutation flowshop problem. OMEGA, Vol. 19 (1), 64–67 (1990).
- [16] R Pugazhenthil and M Anthony Xavier, "Optimization of Permutation Flow Shop with Multi-Objective Criteria." International Journal of Applied Engineering Research, 8(15), (2013), 1807-1813.
- [17] Pugazhenthil, R., and M. Anthony Xavier, "Minimizing Material Processing Time and Idle Time of a Critical Machine in a Flow Shop." In Advanced Materials Research, Trans Tech Publications, 984, (2014) 106-110.
- [18] E. Taillard, Bench Marks for Basic Scheduling Problems, Euro. J. Op. Res. 64(2) (1993) 278-285.