



Nuclear power plant sensor fault detection using singular value decomposition-based method

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Abstract. In a nuclear power plant, periodic sensor calibration is necessary to ensure the correctness of measurements. Those sensors which have gone out of calibration can lead to malfunction of the plant, possibly causing a loss in revenue or damage to equipment. Continuous sensor status monitoring is desirable to assure smooth running of the plant and reduce maintenance costs associated with unnecessary manual sensor calibrations. In this paper, a method is proposed to detect and identify any degradation of sensor performance. The validation process consists of two steps: (i) residual generation and (ii) fault detection by residual evaluation. Singular value decomposition (SVD) and Euclidean distance (ED) methods are used to generate the residual and evaluate the fault on the residual space, respectively. This paper claims that SVD-based fault detection method is better than the well-known principal component analysis-based method. The method is validated using data from fast breeder test reactor.

Keywords. Sensor fault; fast breeder test reactor; singular value decomposition; Euclidean distance.

1. Introduction

A nuclear power plant (NPP) has a large number of sensors to monitor different parameters such as temperature, pressure and flow rate of the process fluid. As the operational decisions depend on sensor signals, it is necessary that the signal produced by the sensor must be faithful. Sensors will undergo physical degradation due to ageing, which results in their readings deviating from the actual value or the calibration curve. Some early indications of sensor fault can take the form of a lagging response caused by the increase of the sensor time constant. Other early signs of a sensor fault may consist of occasional inconsistent output due to loose sensor component contacts. A conventional method of maintenance for the sensors showing signals out of the allowable range consists of off-line integrity evaluation and recalibration or replacement. This approach does not result in timely detection of sensor degradation because inspection has to wait for their scheduled process to shutdowns. The objective of online sensor monitoring is to detect early indications of a sensor fault, thus enabling predictive maintenance.

1.1 Related work

Several techniques have been suggested for sensor fault detection and diagnosis (FDD) in the literature. These methods can be broadly classified into two categories: model-based and data-driven methods. In model-based methods, faults are detected and isolated by residual generation and evaluation. The model describes the mathematical and systematic characteristics of the process. In these methods, fault is detected by comparing the actual output with information obtained from the model. Kalman filter (KF) model-based method was used for fault detection and isolation (FDI) in a dynamic system [1]. It has a systematic design, noise disposal and enhances sensitivity to produce the effective results. Zarei and Poshtan [2] proposed a sensor FDI scheme based on the Luenberger Observer method. Gertler [3] established a dynamic parity relation to detect and isolate the system faults systematically and integrally. Bayesian Belief Network (BBN) and multi-stage BBN models were developed for fault detection and diagnosis (FDD) in a transient or steady-state system [4]. The success of the aforementioned methods depends on the fidelity of the system or the component model expressed in a mathematical form. However, for some complex processes, it is very difficult to obtain a highly accurate mathematical model.

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On the other hand, the data-driven methods are developed using historical data. Well-known data-driven methods for sensor malfunction detection are principal component analysis (PCA) and its extensions. Wang and Cui [5] have developed a method for sensor FDD using PCA. They utilised Q-statistic and Q-contribution plot to detect the fault. A non-linear approach of PCA was proposed by Huang *et al* [6] for sensor and actuator fault in non-linear systems. Wang and Xiao [7] have invented a technique for air handling unit (AHU) system sensor data validation using PCA, where Q-statistic or squared prediction error was used to set the threshold and the fault is fixed by Q-contribution plot. However, PCA is not aware of the pattern. It finds the relation between the variables, and that may produce false alarms. Several ANN approaches were developed to design sensor FDD in different industrial control systems. The ANN was used to predict the correlated variable in NPPs for sensor fault detection and plant monitoring [8]. Auto-associative neural network (AANN) was proposed for engine control system's sensor fault diagnosis and reconstruction [9]. NN-based classification scheme was used to recognise the sensor drift in Gas Turbine systems [10]. A dual NN strategy was designed in AHUs for sensor fault detection and its efficiency analysis [11]. Cascade NN (CNN) was used for sensor fault detection and identification [12]. The NN and KF schemes for sensor validation were proposed for flight control systems [13]. The FDI technique was developed by integrating two successful data-driven methods, PCA and NN by Zhou *et al* [14]. The combination of wavelet and fractal analysis with NN scheme was designed by Zhu *et al* [15] in the AHU system sensor FDD. A hybrid of data-driven soft measurement and modeling method was proposed for power plant sensor condition monitoring [16]. This method includes generalised regression neural network (GRNN), mean impact value (MIV), partial least squares regression (PLSR) and B-Spline transformation techniques. Hou *et al* [17] designed a method utilising data mining principle for sensor validation in air-conditioner systems using rough set (RS) and ANN. Training the network using the neural network and its combination method was time-consuming.

1.2 Motivation and contribution of this paper

In data-driven methods, sensor fault detection is based on calculating metrics that are used to detect the fault. Numerous metrics are used to identify the fault along with the PCA method that includes the Hotelling T^2 -statistic [18] and the Q-statistic [19]. The T^2 -statistic is used to estimate the maximum variation captured by the principal components, whereas the Q-statistic is used to calculate the deviation of the residual that are not captured by the principal components. Wang and Chen [20] noticed that the T^2 -statistic value exceeds the threshold in nominal process condition and produces false alarms.

As pointed out by Romagnoli and Palazoglu [19], the T^2 -statistic will not detect the actual fault because the compact space is sometimes unable to capture small variation in the data. The Q-statistic will detect the fault by computing the square of the error between the actual data and its redundancy [21]. So it is more sensitive than T^2 -statistic. Again, the performance of Q-statistic depends on the redundancy of the data. The data redundancy or reconstruction is based on the choice of the number of principal components. If the principal components are under- or over-estimated, the Q-statistic creates false alarms. The Q-statistic is seriously affected if the eigenvalues of the covariance matrix are roughly equal. It produces an effective result if the first eigenvalue is large and the remaining are very small when the eigenvalues are sorted in decreasing order. Thus, the Q-statistic will not always produce good results.

Recently, Jha and Yadav [22] reported that the SVD is more effective than the PCA for denoising the signals. In this work, the SVD method is used to overcome the PCA reconstruction problem. The SVD reconstruction is not affected by the type of eigenvalues, because in the SVD, the first singular value is always very large (for sensor data) and others are very small. The fault detection metric is applied to the difference between the training and the testing residual, but not directly to the residual. The fault is detected if the distance between the mean of the training and the testing residual crosses the threshold value. The Euclidean distance and the Mahalanobis distance are applied to estimate the distance between two vectors or matrices. If the variable variation is taken into account, the Mahalanobis distance is better than the Euclidean distance. Each sensor variation is approximately same in the fast breeder test reactor (FBTR). So, the Euclidean distance is proposed as a fault detection metric.

This paper is organised into five sections including the present one. The next section presents the proposed SVD-based method for sensor fault detection. The brief description about the FBTR is given in section 3. Section 4 explains the PCA-based fault detection method using Hotelling T^2 -statistic and Q-statistic. Results obtained with the proposed method are compared with the existing PCA-based method and elaborated in section 5. The final conclusion of the paper and recommendations for future research work are given in section 6.

2. Proposed method

The SVD is an important tool in signal processing and statistical analysis. An important feature of SVD is its feature extraction capability. In this paper, extraction property of SVD is applied to detect a sensor fault in NPP. The proposed method consists of two steps: (i) residual generation and (ii) residual evaluation. Residual is generated using the SVD tool by projecting the original data into

a new base set. The deviation of approximate of data from the original is the residual. The fault is detected by computing the distance between training and test residual. The Euclidean distance is imposed to calculate the distance between two matrices. The block diagram of the proposed method is given in figure 1.

2.1 Residual generation by SVD

SVD is an effective tool for feature extraction and compression. It factorises the given matrix into a singular value and singular vector matrices. Any matrix, $X \in R^{m \times n}$, where $m > n$, can be decomposed as

$$X = U \Sigma V^T \quad (1)$$

where U is an $m \times m$ left singular vector, V is an $n \times n$ right singular vector and Σ is an $m \times n$ diagonal matrix with singular values in descending order i.e. $\lambda_{11} > \lambda_{22} > \dots > \lambda_{nm}$. The left and right singular vectors are the eigenvectors of XX^T and $X^T X$, respectively. The singular vectors are orthogonal. If the Σ is written as

$$\Sigma = \begin{bmatrix} \lambda_{11} & \dots & 0 \\ \vdots & \ddots & \vdots \\ 0 & 0 & \lambda_{nm} \end{bmatrix} = \begin{bmatrix} \lambda_{11} & \dots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \dots & 0 \end{bmatrix} + \dots + \begin{bmatrix} 0 & \dots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \dots & \lambda_{nm} \end{bmatrix} \quad (2)$$

then Eq. (1) can be re-written as

$$X = \sum_{i=1}^n u_{mi} \lambda_{ii} v_{ni}^T. \quad (3)$$

The SVD approach operates by projecting the original data onto a new basis, which captures the original features. By Eq. (3), the data can be reconstructed by selecting important singular values. The goodness of the SVD-based fault detection depends on an accurate selection of principal singular values. Over- and underestimation of the number of singular values can initiate noise that disguises the important features and omits important variations in the data, which degrades the reconstruction by SVD. So, it is important to choose appropriate principal singular values. Like PCA, important singular values can be selected by the cumulative percent variance [23], parallel analysis, sequential tests [24], etc. In this paper, principal singular values are selected by

the cumulative percent variance that captured over 90% of the cumulative sum of the eigenvalues.

If the number of principal singular value k is determined, the dimension of the singular vectors and singular value matrices are truncated into k dimension as $U_{m \times k} \in R^{m \times k}$, $V_{n \times k} \in R^{n \times k}$ and $\Sigma_{k \times k} \in R^{k \times k}$.

The data can be reconstructed by multiplication of the truncated matrices:

$$\bar{X}_{m \times n} = U_{m \times k} \times \Sigma_{k \times k} \times V_{n \times k}^T. \quad (4)$$

Residual or error is generated by the difference of the original data X and reconstructed data \bar{X} , as

$$E = |X - \bar{X}|. \quad (5)$$

2.2 Residual evaluations

The main objective of data reconstruction is to remove noise or outlier and approximate to a normal data. A fault-free data set is used to train the model, therefore, the elements of the training error matrix are very small (near to zero). If the test data matrix has any anomaly (anomalies), then there is a deviation between actual and reconstructed data, and the elements of the test residual matrix are high compared to the training residual matrix. The faults or anomalies are detected by calculating element-wise distance between the test residual and the mean of the training residual. If the distance exceeds the threshold value, then there exists a fault. Statistical techniques are applied to calculate the element-wise distance between two matrices. The Euclidean distance [25] between the points $x = (x_1, \dots, x_p)^T$ and $y = (y_1, \dots, y_p)^T$ in the p -dimensional space is defined as

$$d_{ED}(x, y) = \sqrt{(x_1 - y_1)^2 + \dots + (x_p - y_p)^2} = \sqrt{(x - y)^T (x - y)} \quad (6)$$

The Mahalanobis distance [25] between two points $x = (x_1, \dots, x_p)^T$ and $y = (y_1, \dots, y_p)^T$ in the p -dimensional space is defined as

$$d_{MD}(x, y) = \sqrt{(x - y)^T S^{-1} (x - y)} \quad (7)$$

where S is the covariance matrix of X .

Both the methods are efficient for calculating the distance between two points, but the Mahalanobis distance employs covariance. If the covariance is one, then both are identical, and if the covariance or variance varies from variable to variable, then the Mahalanobis distance will be effective. In FBTR, each sensor variation is approximately the same, and hence the Euclidean distance is applied to compute the distance between the test error matrix and the mean of the training error matrix.

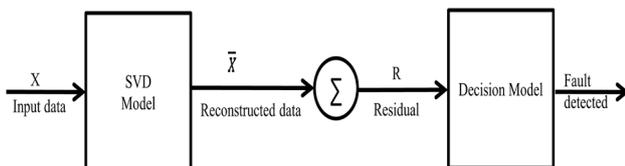


Figure 1. SVD model for sensor fault detection.

Table 1. Different sensors in primary sodium circuit.

Sensor application region	Sensor name	No. of sensors
Inlet sodium temperature	Cromel-Alumel thermocouple	3
Outlet sodium temperature	Cromel-Alumel thermocouple	172
Primary sodium flow	Eddy current flow meter	6

4.1b *Q*-statistics: The *Q*-statistic measures the square of error not captured by principal components in approximation. It is defined as

$$Q = \|E\|^2 = \|x(\mathbf{I} - \hat{\mathbf{V}}\hat{\mathbf{V}}^T)\|^2 \quad (12)$$

Whenever a new test data is available, the *Q*-statistic value is estimated and it is compared to a threshold Q_α defined as

$$Q_\alpha = \theta_1 \left[\frac{c_\alpha h_0 \sqrt{2\theta_2}}{\theta_1} + 1 + \frac{\theta_2 h_0 (h_0 - 1)}{\theta_1^2} \right]^{\frac{1}{h_0}} \quad (13)$$

where c_α is the standard normal distribution with α significance level, θ_i and h_0 are defined as follows:

$$\theta_i = \sum_{j=l+1}^N \lambda_j^i, \quad h_0 = 1 - \frac{2\theta_1\theta_3}{3\theta_2^2}$$

where N is the number of variables. If the *Q*-statistic exceeds Q_α , the fault is detected.

5. Result and discussion

This section presents the results for sensor fault detection in the primary sodium circuit system of the nuclear reactor using the proposed SVD method and the existing PCA

method. In the primary sodium system, 181 sensors are used and the details are given in table 1. Chromel-Alumel Thermocouples are used for measurement of inlet and outlet sodium temperature and Eddy flow meter is used for measurement of primary sodium flow into the reactor. There are three inlet thermocouples that are located in east, west and middle. The outlet centre fuel sub-assembly has four thermocouples and the remaining 84 sub-assemblies each have two thermocouples.

The results of the proposed method are compared with those of the existing PCA method using the FBTR data samples given in table 2. The sample data have only 14 rows and 5 columns. The actual data may be having 929 rows and 181 columns.

The SVD data approximation is closer to the original than the PCA, because in the PCA, the selected principal components, i.e. the principal eigenvectors, are unable to capture all the important features of the data matrix. The eigenvector corresponding to the smaller eigenvalues carries some important features of the data. The approximation is good if the first eigenvalue is large and the remaining are very small when the eigenvalues are sorted in decreasing order. The approximation is not closer to the original if the eigenvalues are roughly equal. The eigenvalues of the primary sodium circuit's sensor data are of the same order of magnitude, as shown in figure 3. For the SVD method, the first singular value is always very large for the sensor data, and the remaining are negligible. So, the first singular vector captured all the important features of the data matrix. The SVD singular values of the primary sodium circuit's sensor data are shown in figure 4. The reconstruction and residues generated by the SVD and the PCA are shown in figures 5–8.

The Euclidean distance metric is effective for primary sodium circuit sensor fault detection, because the operator has the freedom to set the threshold value by the characteristic of the sensors. In *Q*-statistic, the fault propagates through the model error, the threshold value Q_α is

Table 2. Sample data of the primary sodium system sensors in FBTR.

Date and time	TNA000W	TNA000X	TNA000Y	TNA000Z	TNA001X
05-06-2012#09:53:41	185.67	184.92	184.04	185.04	184.04
05-06-2012#09:53:43	185.78	184.66	183.91	185.03	183.91
05-06-2012#09:53:45	185.81	184.69	184.19	185.19	183.94
05-06-2012#09:53:47	185.42	184.67	184.04	185.17	183.92
05-06-2012#09:53:49	185.67	184.42	183.92	185.04	183.92
05-06-2012#09:53:51	184.92	184.79	184.04	185.04	183.92
05-06-2012#09:53:53	185.79	184.17	184.04	185.17	183.92
05-06-2012#09:53:55	185.66	184.66	184.16	184.91	183.78
05-06-2012#09:53:57	185.79	184.79	184.04	185.17	183.92
05-06-2012#09:53:59	185.78	184.53	183.78	185.16	183.91
05-06-2012#09:54:01	185.53	184.66	184.03	185.16	183.91
05-06-2012#09:54:03	185.54	184.67	184.04	185.04	183.79
05-06-2012#09:54:05	185.79	184.67	183.42	185.17	183.92
05-06-2012#09:54:07	185.28	184.78	183.91	184.91	183.78

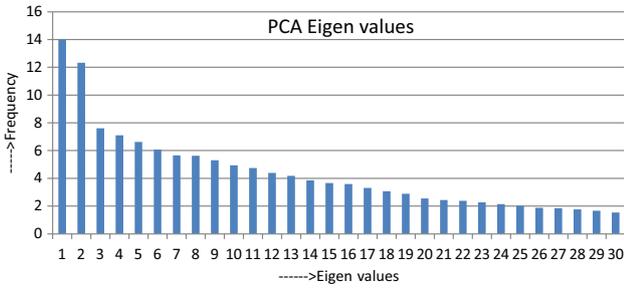


Figure 3. Eigenvalues of the primary sodium circuit sensor data.

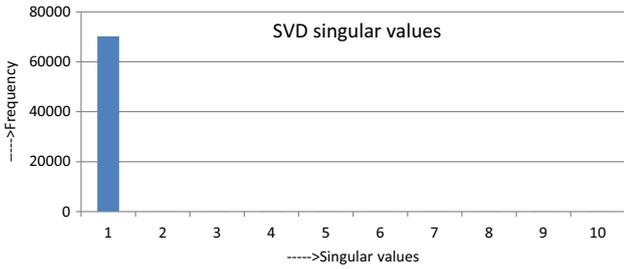


Figure 4. Singular values of the primary sodium circuit sensor data.

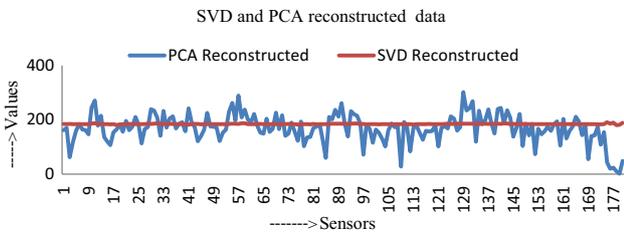


Figure 5. Comparison of reconstruction by SVD and PCA.

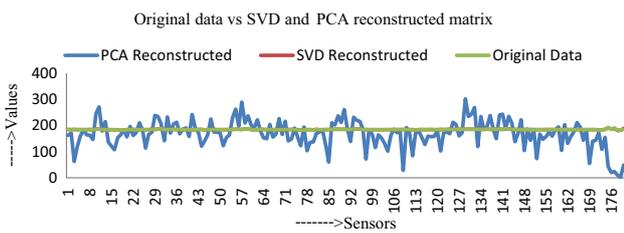


Figure 6. Comparison of reconstruction (by SVD and PCA) and original signals.

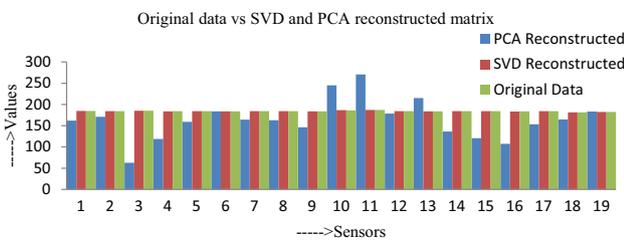


Figure 7. Histogram of reconstructed data by the SVD and the PCA along with original data.

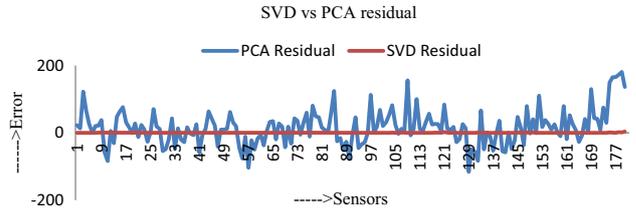


Figure 8. Comparison of the residual of a signal by the SVD and the PCA.

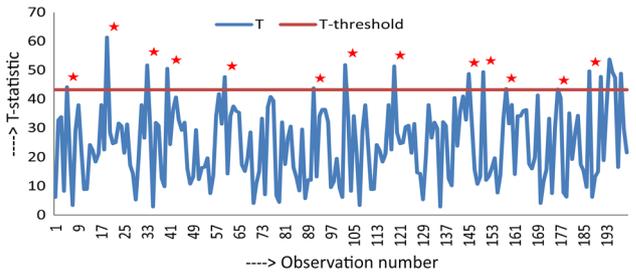


Figure 9. Fault detection using the PCA and T²-statistic.

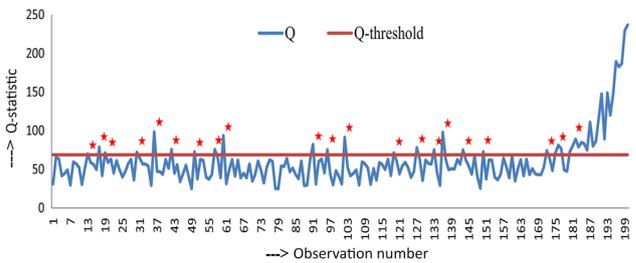


Figure 10. Fault detection using the PCA and Q-statistic.

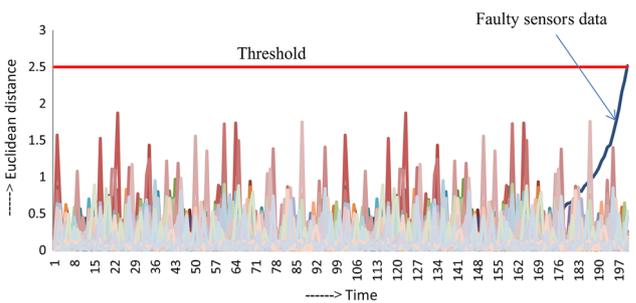


Figure 11. Fault detection using the SVD and Euclidean distance.

dependent on the number of principal eigenvalues and hence the operator has no freedom to set the threshold value. The variation of T-statistic (Hotelling T²-statistic), Q-statistic and the SVD-based Euclidean distance for the same data are shown in figures 9–11. The T²-statistic is unable to detect the actual fault, but raises some false alarms. This is indicated by the red colour star symbol in

figure 9. The Q-statistic is able to detect the actual fault along with some false alarms as shown by the red star symbol in figure 10. The SVD method along with the Euclidean distance detects the actual fault without false alarm.

6. Conclusion and future work

Online monitoring of the sensor's physical condition can avoid many problems associated with manual calibration of sensors. The SVD model is developed for the detection of sensor faults in nuclear power plants. SVD is a simple linear algebraic factorisation method. SVD is used to generate the residual matrix by selecting few largest singular values. The reconstruction matrix is closer to the original data. The Euclidean distance is employed in residual difference space to detect the error length. If the error length exceeds the threshold value, then a fault is detected. In a dynamic process, it is very flexible to change the threshold value. The proposed method will detect and identify the faulty sensor sooner. The accuracy of the fault detection is higher than all the other existing methods and will not produce any false/spurious alarm.

There are some limitations in the reconstruction of the data using the PCA and the SVD methods, and fault detection using these methods. The following are recommended for future work:

- The type of data for which the PCA eigenvalues are roughly equal and the type of the data for which the first eigenvalue is large and remaining are small should be obtained.
- A method to set the threshold value for fault detection from several variables with different variances using the Mahalanobis distance needs to evolve.

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