

A New GT Heuristic for Solving Multi Objective Job Shop Scheduling Problems

D.Lakshmipathy^{1*}, M.Chandrasekaran^{2,b}, T.Balamurugan^{3,c}, P.Sriramya^{4,d}

¹Research Scholar, Dept of Mechanical Engineering, Vels University, Chennai, India

²Professor, Dept of Mechanical Engineering, Vels University, Chennai, India

³Asso. Prof, St.Joesph's College of Engineering, Chennai, India

⁴Asso. Prof, Saveetha School of Engineering, Chennai, India

lakshmipathid@yahoo.co.in (Corresponding author)

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ABSTRACT

The n-job, m-machine Job shop scheduling (JSP) problem is one of the general production scheduling problems in manufacturing system. Scheduling problems vary widely according to specific production tasks but most are NP-hard problems. Scheduling problems are usually solved using heuristics to get optimal or near optimal solutions because problems found in practical applications cannot be solved to optimality using reasonable resources in many cases. In this paper, optimization of three practical performance measures mean job flow time, mean job tardiness and makespan are considered. New Game theory based heuristic method (GT) is used for finding optimal makespan, mean flow time, mean tardiness values of different size problems. The results show that the GT Heuristic is an efficient and effective method that gives better results than Genetic Algorithm (GA). The proposed GT Heuristic is a good problem-solving technique for job shop scheduling problem with multi criteria.

1 INTRODUCTION

The classical job-shop scheduling problem (JSP) is one of most difficult combinatorial optimization problems. During the last decades a great deal of attention has been paid to solving these problems with many algorithms by considering single objective. But real world scheduling problems naturally involve multiple objectives. There are only few attempts available to tackle the multi-objective JSP. In a multi-objective context, find as much different schedules as possible, which are non-dominated with regard to two or more objectives. Some frequently used performance measures are makespan, mean flow-time and mean tardiness. Makespan is defined as the maximum completion time of all jobs. Mean flow-time is the average of the flow-times of all jobs. Mean tardiness is defined as the average of tardiness of all jobs.

2 LITERATURE REVIEW

2.1 Job Shop Scheduling

Brucker [1] show that the Job shop Scheduling (JSP) is an NP-hard [2] combinatorial problem. Because of the NP-hard characteristics of job shop scheduling, it is usually very hard to find its optimal solution, and an optimal solution in the mathematical sense is not always necessary in practices [3]. Researchers turned to search its near-optimal solutions with all kind of heuristic algorithms [4]. Fortunately, the searched near optimal solutions usually meet requirements of practical problems very well.

In a single-objective context some of the recent approaches have shown quite promising results [5-6]. But real world scheduling problems naturally involve multiple objectives. There are only few attempts to tackle the multi-objective JSP [7].

2.2 Graph Theory based (GT) Heuristic

Trees are more important data structures, which come in many forms. Some times trees are static in the sense that their shape is determined before running of the algorithm, and they do not change shape while the algorithm runs. In other cases, trees are dynamic, meaning that they undergo shape changes during the running of the algorithm.

3.2.1 Depth First Search

- ❖ Declare two empty lists: Open and Closed. Add Start node to open list.
- ❖ While Open list is not empty, loop the following:
 - a. Remove the first node from Open List.
 - b. Check to see if the removed node is destination.
- ❖ If the removed node is destination, break out of the loop, add the node to closed list, and return the value of closed list.
- ❖ If the removed node is not destination, continue the loop (go to Step c).
- ❖ Extract the neighbors of above removed node.
- ❖ Add the neighbors to the *beginning* of Open list, and add the removed node to closed list. Continue looping.

3.2.2 Breadth First Search

- ❖ Declare two empty lists: Open and Closed. Add Start node to open list.
- ❖ While Open list is not empty, loop the following:
 - ❖ Remove the first node from Open List.
 - ❖ Check to see if the removed node is destination
 - ❖ If the removed node is destination, break out of the loop, add the node to closed list, and return the value of closed list.
 - ❖ If the removed node is not destination, continue the loop (go to Step c).
 - ❖ Extract the neighbors of above removed node.
 - ❖ Add the neighbors to the *end* of Open list, and add the removed node to closed list.

3.2.3 Tree traversal

In computer science, tree traversal is the process of visiting each node in a tree data structure. Tree traversal, also called walking the tree, provides for sequential processing of each node in what is, by nature, a non-sequential data structure. Such traversals are classified by the order in which the nodes are visited.

If n is a node in a binary search tree, then everything in n 's left subtree is less than n , and everything in n 's right subtree is greater than or equal to n . Thus, the left subtrees in order, using a recursive call, and then visit n , and then visit the right subtree in order. Assume the recursive calls correctly visit the subtrees in order using the mathematical principle of structural induction.

3 PROBLEM FORMULATION

In a multi-objective context, find as much different schedules as possible, which are non-dominated with regard to two or more objectives. Performance measures are makespan, mean flow-time and mean tardiness. Makespan is defined as the maximum completion time of all jobs. Mean flow-time is the average of the flow-times of all jobs. Mean tardiness is defined as the average of tardiness of all jobs.

The combined objective function for the multi objective Job Shop Problem is,

$$\text{COF} = \text{Min} [w_1 (\text{ms}_i/\text{ms}^*) + w_2 (T_i/T^*) + w_3 (\text{mfi}/\text{mf}^*)]$$

Where, $w_1 = (R_1/\sum R)$, $w_2 = (R_2/\sum R)$,

$w_3 = (R_3/\sum R)$ $\sum R = (R_1 + R_2 + R_3)$,

where R_1, R_2, R_3 - Random numbers

ms^* - Make Span Global minimum

T^* - Mean Tardiness Global minimum

mf^* - Mean Flow Time Global minimum

ms_i - Make span Iteration minimum

T_i - Mean Tardiness Iteration minimum

mfi - Mean Flow Time Iteration minimum

w_1, w_2, w_3 - Weightage factors

MFT - Mean flow time,

MT - Mean Tardiness

COF - Combined Objective Function

5 RESULTS AND DISCUSSION

The new heuristic is developed and implemented in C language on personal computer Pentium IV 2.4 GHz. The maximum number of iterations has been set to $100 \times n$, where n is the number of jobs. Multi-objective optimization differs from single-objective optimization in many ways [8]. For two or more conflicting objectives, each objective corresponds to a different optimal solution, but none of these trade-off solutions is optimal with respect to all objectives. Thus, multi-objective optimization does not try to find one optimal solution but all trade-off solutions.

For multi-objective scheduling the proposed new GT heuristic is used to optimize makespan, mean flow time and mean tardiness of the two JSP given by Bagchi [7] are the basis of the following experiments. The first problem, called JSP1, is a ten job five machine instance. The second problem, called JSP2, is a ten job ten machine instance. Apparently, the GT heuristic algorithm minimizes all objectives simultaneously. This GT heuristic is compared with the similar previous work using GA [9] and shown in Table 1 and Table 2.

Notations Used

MS - Makespan, MFT - Mean Flow Time
 MT - Mean Tardiness, COF - Combined Objective Function

Table 1. Results of GT Heuristic with Genetic Algorithm for JSP 1

JSP 1	Genetic Algorithm				GT Heuristic			
	MS	MT	MFT	COF	MS	MT	MFT	COF
1	156	10.8	128.4	0.926	152	16.845	117.8	0.4811
2	158	8.2	126	0.903	162	16.805	111.2	0.3450
3	159	15.7	124.3	0.622	163	15.802	128.5	0.5674
4	159	7.8	127.3	0.773	164	12.97	115.28	0.5714
5	160	13.9	124.3	0.630	168	12.042	114.7	0.3696
6	162	6.4	130.5	0.672	170	14.985	121.65	0.6167
7	165	6.4	128.8	0.867	172	10.442	113.42	0.3861
8	167	15.1	122.4	0.629	170	12.804	119.58	0.6112
9	169	6.1	134.5	0.683	171	7.822	119.91	0.6729
10	182	5.8	135.4	0.632	178	9.759	139.30	0.6023

6 CONCLUSION

In this paper, a new heuristic approach has been used for solving multi objective job shop scheduling problems with the objective of minimization of makespan, mean flow time and mean tardiness. This approach uses simple but effective techniques depth first search, Breadth first search and tree traversal. This approach has been tested on JSP 1 and JSP 2 problem instances given in Bagchi [7]. The findings were compared with Genetic Algorithm [12] that tested the same problems. The New heuristic gives better results than the genetic algorithm. The proposed new heuristic is competent and proves to be a good problem-solving technique for job shop scheduling.

Table 2 Results of GT Heuristic with Genetic Algorithm for JSP 2

JSP 2	Genetic Algorithm				GT Heuristic			
	MS	MT	MFT	COF	MS	MT	MFT	COF
1	196	32.2	174.7	0.726	185	30.605	152.10	0.6821
2	199	33	174.6	0.703	196	31.597	138.2	0.4278
3	201	31.8	176.1	0.622	205	31.910	107.3	0.4805
4	203	32.2	173.4	0.673	206	31.965	166.25	0.3135
5	204	31.3	174.8	0.630	207	32.152	139.7	0.5023
6	212	31.6	174.5	0.602	208	30.086	147.1	0.5950
7	228	30.7	189.1	0.667	210	31.418	135.3	0.4964
8	230	29.3	179.4	0.629	213	31.398	148.31	0.4030
9	238	28.2	188.1	0.683	220	32.413	137.89	0.3899
10	254	29.2	186.7	0.632	224	32.856	135.2	0.4578

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