



Application of Domination Parameters in Network Design

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ABSTRACT

The objective of Network design is to create communication systems that are economical, scalable, dependable and useful. With devices represented as vertices and communication linkages as edges, graph theory offers a strong mathematical framework for modelling and analysing networks. Domination parameters are one of the many graph-theoretic ideas that are important for network structure optimization. These characteristics serve in locating crucial nodes in charge of keeping focus towards managing and preserving network communication. The significance of domination parameters and their uses in network design are covered in this study.

Keywords: Domination, Connected Domination, Roman Domination, Network Design

1. Introduction and Literature Review

Effective techniques for Resource allocation, Routing, Monitoring and Fault management are necessary for modern communication networks such as Wireless Sensor Networks, Mobile and Hoc Networks, Wireless Mesh Networks and Internet Infrastructures. Domination theory is one of the most commonly used topics of graph theory which provides several tools to handle these issues. A subset of vertices in a graph that all of the graph's vertices either belong to or are adjacent to at least one vertex in the subset is known as a dominating set. Network designers can find the best places for control nodes, routers, gateways and monitoring stations by using the quantitative measurements provided by dominance parameters. With several applications in network architecture and communication, dominance theory has become a significant topic of graph theory.

In 1962, Ore who examined the characteristics of dominating sets in graphs and laid the groundwork for later studies explicitly proposed the idea of domination. Since then, Domination theory has expanded into significant field of study and several domination parameters have been created to solve real-world network optimization issues. One of the most extensive descriptions of domination in graphs was given by Haynes, Hedetniemi and Slater in 1998. In addition to establishing several theoretical findings that still direct contemporary research, their work methodically specified domination metrics such as domination number, connected domination, absolute domination and independent domination. It illustrated the use of dominance notions to communication infrastructure development, resource allocation and network coverage. Connected dominating sets are an essential instrument for wireless communication networks.

In 1998, Guha and Khuller sowed the value of approximation methods in network optimization by proposing them for the Minimum Connected Dominating set issues. The development of effective routing methods for extensive communication networks was greatly impacted by their work. A distributed technique for creating connected dominating sets in mobile ad hoc networks was presented by Wu and Li in 1999. Their method increased network scalability and decreased routing overhead which led to the widespread use of Connected Dominating Set based backbone creation in wireless networking. Numerous other studies on energy-efficient routing and topology control were made possible by this study. The effectiveness of connected dominating set creation in wireless ad hoc networks was further enhanced by Alzoubi, Wan and Frieder in 2002. Their algorithm reduced energy consumption and communication costs by minimizing the number of the supporting nodes while maintaining connectivity. Their results illustrated the usefulness of domination-based strategies in actual networks.

In 2004, Dai and Wu studied the use of dominating sets in wireless sensors networks to design an energy-efficient foundation. They demonstrated how network lifetime may be greatly increased while communication coverage is maintained by reducing the size of connected dominating sets. Their study demonstrated how domination parameters and energy optimization are directly related. In 2004, Cockayne et al. presented Roman domination which included fault-tolerant resource allocation techniques to classical domination theory. This idea has been used in research on network resilience where reserve nodes are necessary to keep services functioning in the event of a breakdown. Since Roman Domination in vital infrastructure and communication networks has been fully studied. Due to its usefulness in large-scale and multi-hop networks, Research in distance domination has also attracted a lot of attention. Proper control node placement is made possible by distance-based domination models which also meet latency and coverage requirements. These models are especially applicable to cloud infrastructures, Internet of things environments and wireless sensor networks.

Weighted domination, Resilient domination and energy-aware domination models have been the subject of recent research. These methods take into account real-world limitations such as node energy levels, communication expenses, dependability standards and changing network conditions. The ability of domination-based network design approaches has been further improved by the incorporation of artificial intelligence, machine learning and metaheuristic optimization techniques. Overall, the work shows that domination parameters offer a useful mathematical framework for resolving issues with coverage, connectivity, routing, fault tolerance and resource optimization in network design. In order to meet the problems of next-generation communication systems, their continuing development is still crucial.

2. Domination Parameters in Network Design

This Section describes about the uses of the domination parameters in Network Design.

Domination Number

The minimum number of vertices required to dominate a whole graph is known as the domination number. By selecting the smallest group of nodes that can provide coverage or control over the entire network, this parameter in network design helps reduce infrastructure expenditures. These chosen nodes could serve as monitoring centers, gateways or base stations. Network efficiency and resource consumption can be greatly increased by lowering the number of controlling nodes while preserving complete coverage.

Connected Domination Number

A dominating set whose vertices form an interconnected subgraph is called a connected dominating set. Because it allows for the creation of a virtual framework the associated connected domination number is very significant in communication networks. Such a framework enhances network administration, lowers communication overhead and enables effective routing. In wireless sensor networks and mobile ad hoc networks, connected dominating sets are frequently utilized to create routing infrastructures that use less energy and require fewer routing updates.

Total Domination

Every vertex in the network has to be adjacent to at least one dominating vertex in order for the concept of total domination to take effect. Because even dominating vertices rely on nearby dominating vertices, this feature improves network resilience. Therefore, Total domination is inappropriate for critical communication systems where stable connectivity is essential since it supports redundancy and fault tolerance.

Independent Domination

The characteristics of independence and domination are combined in independent domination. No two dominating vertices are adjacent in an independent dominating set. Because it disperses control nodes throughout the network and reduces signal interference, this feature is advantageous in wireless communication networks. To promote balanced resource use, access points, cluster heads and communication controllers are often positioned using independent domination.

Distance Domination

Through enabling a dominating vertex to cover nodes within a certain number of hops, distance domination expands on the idea of domination. In large-scale communication systems, when immediate connection between nodes might not always be possible, this value is especially helpful. Distance domination maintains acceptable levels of accessibility and communication delay while lowering deployment costs. Cloud infrastructures, distributed computer systems and multi-hop wireless networks are examples of applications.

Roman domination

Numerous types of responsibility are established among network nodes via Roman domination. In order to help neighbouring nodes in the event of a failure, some nodes are given extra resources or restore capabilities. This idea is useful when creating robust communication networks that can continue to function even in a scenario of unpredictable interruptions. Roman domination is often applied in military communication systems, critical infrastructure networks and disaster recovery plans.

3. Applications in Modern Networks

In present network design, domination parameters have many real-world uses. They are employed in the development of wireless sensor networks, mobile ad hoc networks, cluster-head selection, wireless local area networks, access point placement, infrastructure networks, monitoring station deployment and large-scale communication systems routing optimization. They are essential tools for network engineers and researchers because of their capacity to reduce expenses while guaranteeing coverage, connectivity and dependability. Numerous optimization issues linked to domination such as

Minimum Dominating set and Minimum Connected Dominating set problems are computationally challenging and fall under the category of NP-hard problems. In order to find effective answers, researchers keep creating approximation algorithms, heuristic approaches, evolution algorithms and machine learning-based strategies. It is anticipated that future studies will concentrate on energy-aware domination models, dynamic networks and intelligent network management systems that can adjust to shifting conditions.

4. Conclusion

A fundamental structure for creating dependable and effective communication networks is provided by domination parameters. They are helpful in the optimization of resource allocation, fault tolerance, routing, coverage and connectivity. Domination theory makes it possible to build scalable and affordable network topologies by identifying will continue to be crucial tools for tackling the difficulties of present-day network design and administration as communication technologies progress.

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