

Coordinating Supply Chain Inventory Model for Deteriorating Products

M. Ravithammal, M. Babu, G. Rasitha Banu, P. Muniappan

Abstract: *The paper manages an optimal inventory replenishment policy for a deteriorating item with two part coordination technique (coordination and non coordination). The aim of this model is to determine the optimal values for every strategy such that the expected total cost is minimized. The model is solved analytically to get the ideal solution. It is then outlined with the assistance of numerical models.*

Keywords: *Inventory, Order quantity, Deteriorating products, Coordination*

I. INTRODUCTION

The EOQ and EPQ stock models have been utilized in numerous viable applications on the grounds that these stock models are basic and simple to actualize in associations. The sole goal of the model is to limit the complete stock related costs, normally holding expense and requesting cost. In many situations, these models don't think about the nearness of inadequate items in the part and modify of them. Also, these models have one significant element which is their vigor as for little changes in the parameters. In any case, the EOQ and EPQ stock models have a few presumptions that are exceptionally prohibitive. One of them is that the assembling procedure essentially creates great quality items. Truth be told, there are numerous circumstances practically speaking where the assembling procedure produces flawed items because of reasons, for example, aptitude level of the laborers, machine capacity, defective crude materials and upkeep arrangements.

Federgruen and Yang [1] created ideal inventory enhancement under general supply risks. Hemamalini et al. [2] read EOQ stock model for purchaser seller with screening, arranged expense and controllable lead time. Khan et al. [5] considered an incorporated store network model with blunders in quality review and learning in production. Khang and Fujiwara [6] examined optimality of myopic ordering policies for stock model with stochastic inventory. Mari Selvi et al. [8] contemplated seller purchaser incorporated stock model for controllable lead time with screening and arranged expense. Muniappan et al. [9]

investigated EPQ stock model for falling apart items including partially accumulated deficiencies. Jaber et al. [4] studied an entropic economic order quantity for things with defective quality. J. T. Hsu and L.F. Hsu [3] built up an EOQ model with imperfect quality things, examination blunders, shortage backordering, and deals returns. Khanna et al. [7] read vital creation displaying for defective items with defective investigation process, adjust, and deals return under two-level trade credit. Sarkar and Moon [10] investigated an EPQ model with expansion in a imperfect production system.

II. ASSUMPTIONS AND NOTATIONS

The model utilize the subsequent notations and assumptions

Notations

- D Demand rate
- r_1 Unit ordering cost for Buyer
- r_2 Unit setup cost Vendor
- P Production cost
- Q Economic Order Quantity
- h_b Unit holding cost Buyer
- h_v Unit holding cost Vendor
- C_s Unit screening cost Vendor
- C_d Disposed cost
- n Vendor's multiples of order
- s Shortage cost
- k Buyer's multiples of order
- d Discount factor
- p Purchase cost
- u Percentage of defecting items
- v Percentage of scrap items

Assumptions

- (i) Demand rate is steady.
- (ii) Vendor fabricates the items and buyer having shortage for non coordination technique.
- (iii) For bulk purchase, vendor gives quantity discount to the buyer for coordination method.
- (iv) Also, for coordination method buyer screened or disposed the harmed items and have no shortages and for non coordination method

Revised Manuscript Received on December 5, 2019.

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vendor screened or disposed the harmed items.

III. MODEL FORMULATION

Case (i) : Non-Coordination Model

In non coordination, the total cost for buyer contains following three costs

- i) ordering cost $\frac{r_1 D}{Q}$,
- ii) holding cost $\frac{h_b Q^2}{2Q}$ and
- iii) shortage cost $\frac{s(Q-Q_1)^2}{2Q}$.

Now, the buyer cost will be written as

$$TC_b = \frac{r_1 D}{Q} + \frac{h_b Q^2}{2Q} + \frac{s(Q-Q_1)^2}{2Q} \quad (1)$$

In non coordination, the total cost for vendor contains following five costs

- i) setup cost $\frac{r_2 D}{nQ}$,
- ii) holding cost $\frac{h_v(n-1)Q}{2} \left(\frac{P-D}{P} \right)$,
- iii) disposed cost $\frac{uvC_d nQ}{2}$,
- iv) screening cost $\frac{C_s Q}{2}$ and
- v) transportation cost $F + VQ$.

The vendor cost will be written as

$$TC_v = \frac{r_2 D}{nQ} + \frac{(n-1)h_v Q}{2} \left(\frac{P-D}{P} \right) + \frac{uvC_d nQ}{2} + \frac{C_s Q}{2} + F + VQ \quad (2)$$

For optimality $\frac{\partial TC_b}{\partial Q_1} = 0$ and $\frac{\partial^2 TC_b}{\partial Q_1^2} > 0$ and $\frac{\partial TC_v}{\partial Q} = 0$ and $\frac{\partial^2 TC_v}{\partial Q^2} > 0$

we get, $Q_1^* = \frac{sQ}{h_b + s}$ and

$$Q^* = \sqrt{\frac{2r_1 D}{n[k(n-1)h_v \left(\frac{P-D}{P} \right) + nuvC_d + 2V]}}$$

Hence for non coordination the optimal order size is

$$Q^* = \sqrt{\frac{2r_1 D}{n[k(n-1)h_v \left(\frac{P-D}{P} \right) + nuvC_d + 2V]}}$$
 and the buyer and vendor costs are TC_b^* and TC_v^*

Case (ii): Coordination Model

In coordination, the total cost for buyer contains following four costs

- i) ordering cost $\frac{r_1 D}{Q}$,
- ii) holding cost $\frac{h_b Q^2}{2Q}$,
- iii) screening cost $\frac{C_s Q}{2}$ and
- iv) disposed cost $\frac{uvC_d nQ}{2}$.

Now, the buyer cost will be written as

$$TC_{b1} = \frac{r_1 D}{Q} + \frac{h_b Q^2}{2Q} + \frac{C_s Q}{2} + \frac{uvC_d nQ}{2} \quad (3)$$

In coordination, the total cost for vendor contains following four costs

- i) setup cost $\frac{r_2 D}{nkQ}$,
- ii) holding cost $\frac{h_v k(n-1)Q}{2} \left(\frac{P-D}{P} \right)$,
- iii) transportation cost $F + VQ$ and
- iv) Discount factor pDd .

Now, the vendor cost will be written as

$$TC_{v1} = \frac{r_2 D}{nkQ} + \frac{k(n-1)h_v Q}{2} \left(\frac{P-D}{P} \right) + F + VQ + pDd \quad (4)$$

For optimality $\frac{\partial TC_{v1}}{\partial Q} = 0$ and $\frac{\partial^2 TC_{v1}}{\partial Q^2} > 0$

$$Q^* = \sqrt{\frac{2r_2 D}{nk[k(n-1)h_v \left(\frac{P-D}{P} \right) + 2V]}}$$

Hence for non coordination the optimal order size is

$$Q^* = \sqrt{\frac{2r_2 D}{nk[k(n-1)h_v \left(\frac{P-D}{P} \right) + 2V]}}$$
 and the buyer and vendor costs are TC_{b1}^* and TC_{v1}^*

IV. NUMERICAL EXAMPLE

Example 1: Let $R_1 = 100$, $R_2 = 400$, $D = 1500$, $P = 2500$, $H_v = 0.03$, $H_b = 0.02$, $C_s = 0.1$, $s = 0.25$, $C_d = 0.6$, $u = 0.2$, $v = 0.1$, $p = 0.4$, $n = 2$, $k = 3$, $d(k) = 10\%$, $F=0.1$, $V=0.2$.

The optimal solutions are

Non coordination: $Q^* = 1066$, $Q_1^* = 987.04$,

$TC_b = 150.58$, $TC_v = 562.95$

Coordination: $kQ^* = 2314.6$, $TC_{b1} = 298.58$, $TC_{v1} = 416.80$

Example 2: Let $R_1 = 200$, $R_2 = 500$, $D = 1000$, $P = 1500$, $H_v = 0.05$, $H_b = 0.04$, $C_s = 0.1$, $s = 0.25$, $C_d = 0.6$, $u = 0.2$, $v = 0.1$, $p = 0.4$, $n = 2$, $k = 3$, $d(k) = 10\%$, $F=0.1$, $V=0.2$.

The optimal solutions are

Non coordination: $Q^* = 961$, $Q_1^* = 829.04$, $TC_b = 224.56$, $TC_v = 520.04$

Coordination: $kQ^* = 2070.2$, $TC_{b1} = 428.88$, $TC_{v1} = 370.45$

V. CONCLUSION

In this paper, vendor – buyer EPQ model is created under coordination and non coordination circumstance. For coordination strategy purchaser screened or arranged the harmed things and have no deficiencies and for non coordination technique seller screened or arranged the harmed things. Under coordination, vendor gives quantity discount to the buyer for mass buy. Our point is to process the idea order quantity to minimize the total inventory cost. To contrast and non coordination, coordination circumstance demonstrates more advantages. For the further looks into, our proposed model can be stretched out into multilevel products, one time discount, price discount and temporary discount etc.,

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