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# **Independent Domination Number for some Special types of Snake Graph**

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Abstract--Let G(V,E) be a graph, V has a subset C, contains vertices with atleast one vertex in V that is not in C, then G has the dominating set C.If C has vertices that is not adjacent to one another, then G has an independent dominating set C and so the number of vertices present in the set C represents the IDN, the minimum cardinality of the sets C.In this paper, we were going to deal with Snake graphs in specific, Alternate Triangular and Alternate Quadrilateral Snake graphs. Keeping the concepts of these graphs as our base we extend our paper by defining n-Alternative Triangular Snake graphnA(T<sub>n</sub>),n-Alternative Double Triangular Snake graph  $nA(D(T_n))$ , n-Alternative Quadrilateral Snake graph $nA(Q_n)$  and n-Alternative Double Quadrilateral Snake graphnA( $D(Q_n)$ ). Further we obtain independent domination number for some special types of snake graphs, in particular n-Alternative Triangular Snake graph  $nA(T_n, n-Alternative Double Triangular Snake graph <math>nA(D(T_n))$ , n-Alternative Quadrilateral Snake graph  $nA(Q_n)$  and n-Alternative Double Quadrilateral Snake graphnA( $D(Q_n)$ ).

**Keywords**-Domination set, ID, IDN,  $T_n$ ,  $A(T_n)$ ,  $D(T_n)$ ,  $A(D(T_n))$ ,  $Q_n$ ,  $A(Q_n)$ ,  $D(Q_n)$ ,  $A(D(Q_n)).$ 

#### **1. INTRODUCTION**

In the past the ideas of domination, is started with the game of chess. Later the work was extended by various peoples as, Ahrens in 1901 [16] Berge in 1958 [2] and ore in 1962 [9], by 1972 Cockayne and Hedetniemi [3,4] gone through domination and commenced to review it, tereby a survey was published in 1975 and there came into existence for the topic independent domination number. Thereon, many researchers started to work in that. Thus, Goddard et al. [13,15], Kostichka [1] and Lam et al. [10] gone through regular graph and cubic graph. While Favaron [8] done under general graphs, gave its sharp upper bounds and Haviland [7] extended it. Cockayne et al. [5] found its boundary and its complement, while Shiu et al. [14] gave for trianglefree graphs and thereby characterizing its upper bounds.

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*Definition 1.* [11] Let G(V,E) be a graph, V has a subset C, contains vertices with atleast one vertex in V that is not in C, then G has the dominating set C.

*Definition 2.* [1] If C has vertices that is not adjacent to one another, then G has an independent dominating set C and so the number of vertices present in the set C represents the IDN, the minimum cardinality of the sets C.

Definition 3. [12] Triangular snake( $T_n$ ):

In the path  $P_n$  we add a vertex corresponding to each edge to form a triangle  $C_3$ .

Definition 4. [12] Alternate triangular snake $A(T_n)$ :

In the path  $a_1, a_2, ..., a_n$  we add a vertex  $v_i$  to  $a_i$  and  $a_{i+1}$  (alternately). So that each alternate edge form a triangle  $C_3$ .

Definition 5. n-Alternate triangular snake $nA(T_n)$ :

In the path  $a_1, a_2, ..., a_n$  we add a new vertex  $v_i$  to  $a_i$  and  $a_{i+1}, a_{i+1}$  and  $a_{i+2}, ..., a_{i+(n-1)}$  and  $a_{i+n}$  (n-alternately). So that each n-alternate edge form a triangle  $C_3$ .

Definition 6. [12] Double Triangular snake $D(T_n)$ :

 $D(T_n)$  consists of two  $T_n$  which has a common(standard) path.

*Definition 7.* [12] Alternate Double triangular snake  $A(D(T_n))$ :

 $A(D(T_n))$  consists of two  $A(T_n)$  which has a common(standard) path.

Definition 8. n- Alternate Double triangular snake  $nA(D(T_n))$ :

 $nA(D(T_n))$  consists of two  $nA(T_n)$  which has a common (standard)path.

*Definition 9.* [7] Quadrilateral snake $Q_n$ :

In the path  $a_1, a_2, ..., a_n$  we add a new vertices  $b_i$  and  $c_i$  corresponding to the edges of the path  $a_i$  and  $a_{i+1}$  and by joining  $b_i$  and  $c_i$  for i=1,2,...n-1, we get a cycle  $C_4$ .

Definition 10. [7] Alternate quadrilateral snake $A(Q_n)$ :

In the path  $a_1, a_2, ..., a_n$  we add a new vertices  $b_i$  and  $c_i$  corresponding to the edges of the path  $a_i$  and  $a_{i+1}$  and by joining  $b_i$  and  $c_i$  for  $i \equiv 1 \pmod{2}$  and  $I \leq n-1$  then joining  $b_i$  and  $c_i$  alternatively we get a cycle  $C_4$ .

Definition 11. n-Alternate quadrilateral snake $nA(Q_n)$ :

In the path  $a_1, a_2, ..., a_n$  we add new vertices  $b_i$  and  $c_i$  corresponding to the edges of the path  $a_i$  and  $a_{i+1}, a_{i+1}$  and  $a_{i+2}, ..., a_{i+(n-1)}$  and  $a_{i+n}$  and by joining  $b_i$  and  $c_i$  for  $i \equiv 1 \pmod{3}$  derivatively we get a cycle  $C_4$ .

*Definition 12.* [7] Double Quadrilateral snake $D(Q_n)$ :

 $D(Q_n)$  is obtained from two parallel  $Q_n$  with a common (standard)path.

Definition 13. [7] Alternate Double quadrilateral snake $A(D(Q_n))$ :

 $A(D(Q_n))$  is obtained from two parallel  $A(Q_n)$  with a common (standard)path.

Definition 14. n- Alternate Double quadrilateral snake $nA(D(Q_n))$ :

 $nA(D(Q_n))$  is obtained from two parallel  $nA(Q_n)$  with a common(standard) path.

Section-1

## IDN in

(i)  $2A(T_n)$  (ii)  $3A(T_n)$ (iii)  $4A(T_n)$ (iv)  $5A(T_n)$ 

Theorem 1.1:

Let us take the graph  $2A(T_n)$  with the path  $P_n$ , then  $i(2A(T_n)) = \left|\frac{n}{4}\right|$ 

#### **Proof**:

Procedure for  $2A(T_n)$ :

The  $2A(T_n)$  graph is defined by adding a new vertex for every two edges of  $v_{i-1}$ ,  $v_i$  and  $v_i$ ,  $v_{i+1}$  alternatively.

We label the root path of the vertices as  $v_1, v_2, ..., v_n$  thereby we add a vertex  $a_1, a_2$  to the corresponding edges  $v_1, v_2$  and  $v_2, v_3$  respectively.

Leave the next two edges  $v_3$ ,  $v_4$  and  $v_4$ ,  $v_5$ .

This Alternative process from the vertex  $v_1$  to the vertex  $v_5$  is named as  $A_1$  [1<sup>st</sup> alternative].

Again, add two new vertex  $a_3$ ,  $a_4$  to the corresponding edges  $v_5$ ,  $v_6$  and  $v_6$ ,  $v_7$ . This Alternative process from the vertex  $v_1$  to the vertex  $v_7$  is named as  $A_2$  [2<sup>nd</sup> alternative].

Leave the next two edges  $v_7$ ,  $v_8$  and  $v_8$ ,  $v_9$ .

Continue this process till  $A_n$ .

This graph is named as G and now we find the set C (ID set) for a graph  $2A(T_n)$ , such that V-C has vertices which is adjacent to atleast one vertex in C and thus the vertices in C are independent.

The process goes in such a way, so that we get the IDN for  $2A(T_n)$  as (i.e.,)

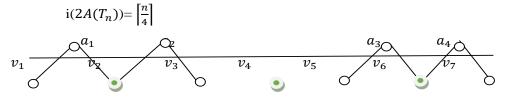


Fig. (1)

Theorem 1.2:

Let us take the graph  $3A(T_n)$  with the path  $P_n$ , then  $i(3A(T_n)) = \left\lfloor \frac{n}{4} \right\rfloor$ 

#### **Proof**:

Procedure for  $3A(T_n)$ :

The  $3A(T_n)$  graph is defined by adding a new vertex for every three edges of  $(v_{i-1}, v_i), (v_i, v_{i+1})$  and  $(v_{i+1}, v_{i+2})$  alternatively.

We label the root path of the vertices as  $v_1, v_2, ..., v_n$  thereby we add a vertex  $a_1, a_2, a_3$  to the corresponding edges  $(v_1, v_2), (v_2, v_3)$  and  $(v_3, v_4)$  respectively.

Leave the next three edges  $(v_4, v_5), (v_4, v_5)$  and  $(v_5, v_6)$ .

This Alternative process from the vertex  $v_1$  to the vertex  $v_6$  is named as  $A_1$  [1<sup>st</sup> alternative].

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Again, add three new vertex  $a_4$ ,  $a_5$ ,  $a_6$  to the corresponding edges  $(v_6, v_7)$ ,  $(v_7, v_8)$  and  $(v_8, v_9)$ . This Alternative process from the vertex  $v_1$  to the vertex  $v_9$  is named as  $A_2$  [2<sup>nd</sup> alternative].

Leave the next three edges  $(v_9, v_{10}), (v_{10}, v_{11})$  and  $(v_{11}, v_{12})$ .

Continue this process till  $A_n$ .

This graph is named as G and now we find the set C (ID set) from a graph  $3A(T_n)$ , such that V-C has vertices which is adjacent to atleast one vertex in C and thus the vertices in C are independent.

The process goes in such a way, so that we get the IDN for  $3A(T_n)$  as (i.e.,)

$$i(3A(T_n)) = \left|\frac{n}{4}\right|$$

Theorem 1.3:

Let us take the graph  $4A(T_n)$  with the path  $P_n$ , then  $i(4A(T_n)) = \left\lfloor \frac{n}{4} \right\rfloor - N$  where N takes the values -1, -2,-3... twice in the series.

Proof:

Procedure for  $4A(T_n)$ :

The  $4A(T_n)$  is defined by adding a new vertex for every four edges of  $(v_{i-1}, v_i), (v_i, v_{i+1}), (v_{i+1}, v_{i+2})$  and  $(v_{i+2}, v_{i+3})$  alternatively.

We label the root path of the vertices as  $v_1, v_2, ..., v_n$  thereby we add a vertex  $a_1, a_2, a_3, a_4$  to the corresponding edges  $(v_1, v_2), (v_2, v_3) (v_3, v_4)$  and  $(v_4, v_5)$  respectively.

Leave the next four edges  $(v_5, v_6)$ ,  $(v_6, v_7)$   $(v_7, v_8)$  and  $(v_8, v_9)$ .

This Alternative process from the vertex  $v_1$  to the vertex  $v_9$  is named as  $A_1$  [1st alternative].

As in theorem 1.2 we follow the same procedure till  $A_n$ .

This graph is named as G and now we find the set C (ID set) from a graph  $4A(T_n)$ , such that V-C has vertices which is adjacent to atleast one vertex in C and thus the vertices in C are independent.

The process goes in such a way, so that we get the IDN for  $4A(T_n)$  as (i.e.,)  $i(4A(T_n)) = \left[\frac{n}{4}\right]$ -N, where N takes the values -1,-2,-3... twice in the series.

Theorem 1.4:

Let us take the graph  $5A(T_n)$  with the path  $P_n$ , then  $i(5A(T_n)) = \left\lfloor \frac{n}{4} \right\rfloor + N$  where N takes the values 0,1 twice alternatively.

#### **Proof**:

Procedure for  $5A(T_n)$ :

The  $5A(T_n)$  graph is defined by adding a new vertex for every five edges of  $(v_{i-1}, v_i), (v_i, v_{i+1}), (v_{i+1}, v_{i+2}), (v_{i+2}, v_{i+3})$  and  $(v_{i+3}, v_{i+4})$  alternatively.

The rest of the procedure is carried out as in theorem 1.2, till  $A_n$ .

Now this graph is named as G and now we find the set C (ID set) from a graph  $5A(T_n)$ , such that V-C has vertices which is adjacent to atleast one vertex in C and thus the vertices in C are independent.

The process goes in such a way, so that we get the IDN for  $5A(T_n)$  as (i.e.,)

 $i(5A(T_n)) = \left[\frac{n}{4}\right] + N$ , where N takes the values 0,1 twice alternatively.

#### Section-2

## IDN in

(i)  $2A(D(T_n))$ (ii)  $3A(D(T_n))$ (iii)  $4A(D(T_n))$ (iv)  $5A(D(T_n))$ 

Theorem 2.1:

Let us take the graph  $2A(D(T_n))$  with the path  $P_n$ , then  $i(2A(D(T_n)) = \lfloor \frac{n}{4} \rfloor + N$  where N takes -1,-2,-3... thrice in the series.

#### **Proof**:

Procedure for  $2A(D(T_n))$ :

The  $2A(D(T_n))$  graph is defined by adding a new vertex above and below the common path for every two edges of  $v_{i-1}$ ,  $v_i$  and  $v_i$ ,  $v_{i+1}$  alternatively.

We label the root path of the vertices as  $v_1, v_2, ..., v_n$  thereby we add a vertex above the root path as  $a_1, a_2$  and below the root path  $asb_1, b_2$  to the corresponding edges  $v_1, v_2$  and  $v_2, v_3$  respectively.

Leave the next two edges  $v_3$ ,  $v_4$  and  $v_4$ ,  $v_5$ .

This Alternative process from the vertex  $v_1$  to the vertex  $v_5$  is named as  $A_1$  [1<sup>st</sup> alternative].

Again, add a new vertex above the path as  $a_3$ ,  $a_4$  and below he path as  $b_3$ ,  $b_4$ to the corresponding edges  $v_5$ ,  $v_6$  and  $v_6$ ,  $v_7$ . This Alternative process from the vertex  $v_1$  to the vertex  $v_7$  is named as  $A_2$  [2<sup>nd</sup> alternative].

Leave the next two edges  $v_7$ ,  $v_8$  and  $v_8$ ,  $v_9$ .

Continue this process till  $A_n$ .

This graph is named as G and now we find the set C (ID set) from a graph  $2A(D(T_n))$ , such that V-C has vertices which is adjacent to atleast one vertex in C and thus the vertices in C are independent.

The process goes in such a way, so that we get the IDN for  $2A(D(T_n))$  as (i.e.,)

 $i(2A(D(T_n))) = \left[\frac{n}{4}\right] + N$  where N takes -1,-2,-3... thrice in the series.

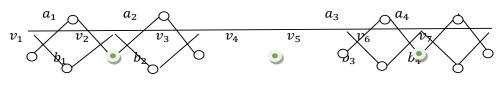


Fig.2:

#### Theorem 2.2:

Let us take the graph  $3A(D(T_n))$  with the path  $P_n$ , then  $i(3A(D(T_n)) = \lfloor \frac{n}{4} \rfloor + N$  where N takes -1,-2,-3... thrice in the series.

# **Proof**:

Procedure for  $3A(D(T_n))$ :

The  $3A(D(T_n))$  graph is defined by adding a new vertex above and below the common path for every three edges of  $(v_{i-1}, v_i), (v_i, v_{i+1})$  and  $(v_{i+1}, v_{i+2})$  alternatively.

We label the root path of the vertices as  $v_1, v_2, ..., v_n$  thereby we add a vertex  $a_1, a_2, a_3$  and  $b_1, b_2, b_3$  above and below the common path the to the corresponding edges  $(v_1, v_2), (v_2, v_3)$  and  $(v_3, v_4)$  respectively.

Leave the next three edges  $(v_4, v_5), (v_4, v_5)$  and  $(v_5, v_6)$ .

Continue this process till  $A_n$  as in theorem 2.1.

This graph is named as G and now we find the set C (ID set) from a graph  $2A(D(T_n))$ , such that V-C has vertices which is adjacent to atleast one vertex in C and thus the vertices in C are independent.

The process goes in such a way, so that we get the IDN for  $3A(D(T_n))$  as (i.e.,)

$$i(3A(D(T_n)) = \left|\frac{n}{4}\right| + N$$
 where N takes -1,-2,-3... thrice in the series.

Theorem 2.3:

Let us take the graph  $4A(D(T_n))$  with the path  $P_n$ , then  $i(4A(D(T_n)) = \left\lfloor \frac{n}{5} \right\rfloor + N$  where N takes -1,0 twice alternatively in the series.

#### **Proof**:

Procedure for  $4A(D(T_n))$ :

The  $4A(D(T_n))$  graph is defined by adding a new vertex above and below the common path for every four edges of  $(v_{i-1}, v_i), (v_i, v_{i+1}), (v_{i+1}, v_{i+2})$  and  $(v_{i+2}, v_{i+3})$  alternatively.

Continue the process as in theorem 2.2 till  $A_n$ .

This graph is named as G and now we find the set C (ID set) from a graph  $2A(D(T_n))$ , such that V-C has vertices which is adjacent to atleast one vertex in C and thus the vertices in C are independent.

The process goes in such a way, so that we get the IDN for  $4A(D(T_n))$  as (i.e.,)

$$i(4A(T_n)) = \left|\frac{n}{5}\right| + N$$
 where N takes -1,0 twice alternatively in the series.

Theorem 2.4:

Let us take the graph  $5A(D(T_n))$  with the path  $P_n$ , then  $i(5A(D(T_n)) = \left\lfloor \frac{n}{4} \right\rfloor + N$  where N takes -1,-2,-3... twice in the series.

#### **Proof**:

Procedure for  $5A(D(T_n))$ :

The  $5A(D(T_n))$  graph is defined by adding a new vertex above and below the common path for every five edges of  $(v_{i-1}, v_i), (v_i, v_{i+1}), (v_{i+1}, v_{i+2}), (v_{i+2}, v_{i+3})$  and  $(v_{i+3}, v_{i+4})$  alternatively.

The rest of the procedure is carried out as in theorem 2.2, till  $A_n$ .

This graph is named as G and now we find the set C (ID set) from a graph  $2A(D(T_n))$ , such that V-C has vertices which is adjacent to atleast one vertex in C and thus the vertices in C are independent.

The process goes in such a way, so that we get the IDN for  $5A(D(T_n))$  as (i.e.,)  $i(5A(T_n)) = \left|\frac{n}{4}\right| + N$  where N takes -1,-2,-3... twice in the series.

#### Section-3

#### IDN in

(i)  $2A(Q_n)$ (ii)  $3A(Q_n)$ (iii)  $4A(Q_n)$  (iv)  $5A(Q_n)$ 

Theorem 3.1:

Let us take the graph  $2A(Q_n)$  with the path  $P_n$ , then  $i(2A(Q_n)) = \left|\frac{n}{2}\right|$ 

#### **Proof**:

Procedure for  $2A(Q_n)$ :

The  $2A(Q_n)$  is defined by adding two new vertices for every two edges of  $v_{i-1}$ ,  $v_i$  and  $v_i$ ,  $v_{i+1}$  alternatively.

We label the root path of the vertices as  $v_1, v_2, ..., v_n$  thereby we add a vertices  $a_1, b_1$  and  $a_2, b_2$  to the corresponding edges  $v_1, v_2$  and  $v_2, v_3$  respectively.

Leave the next two edges  $v_3$ ,  $v_4$  and  $v_4$ ,  $v_5$ .

This Alternative process from the vertex  $v_1$  to the vertex  $v_5$  is named as  $A_1$  [1<sup>st</sup> alternative].

Again, add the vertices  $a_3$ ,  $b_3$  and  $a_4$ ,  $b_4$  to the corresponding edges  $v_5$ ,  $v_6$  and  $v_6$ ,  $v_7$ . This Alternative process from the vertex  $v_1$  to the vertex  $v_7$  is named as  $A_2$  [2<sup>nd</sup> alternative].

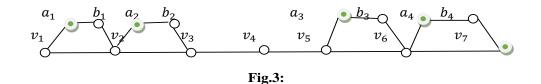
Leave the next two edges  $v_7$ ,  $v_8$  and  $v_8$ ,  $v_9$ .

Continue this process till  $A_n$ .

This graph is named as G and now we find the set C (ID set) from a graph  $2A(Q_n)$ , such that C has vertices which is adjacent to atleast one vertex in C and thus the vertices in C are independent.

The process goes in such a way, so that we get the IDN for  $2A(Q_n)$  as (i.e.,)

$$i(2A(Q_n)) = \left|\frac{n}{3}\right|$$



Theorem 3.2

Let us take the graph  $3A(Q_n)$  with the path  $P_n$ , then  $i(3A(Q_n)) = \left|\frac{n}{2}\right|$ 

#### **Proof**:

Procedure for  $3A(Q_n)$ :

The  $3A(Q_n)$  graph is defined by adding two new vertex for every three edges of  $(v_{i-1}, v_i), (v_i, v_{i+1})$  and  $(v_{i+1}, v_{i+2})$  alternatively.

We label the root path of the vertices as  $v_1, v_2, ..., v_n$  thereby we add the  $a_1b_1, a_2b_2, a_3b_3$  to the corresponding edges  $(v_1, v_2), (v_2, v_3)$  and  $(v_3, v_4)$  respectively.

Leave the next three edges  $(v_4, v_5)$ ,  $(v_4, v_5)$  and  $(v_5, v_6)$ . Continue the process as in theorem 3.1, till  $A_n$ . This graph is named as G and now we find the set C (ID set) from a graph  $3A(Q_n)$ , such that V-C has vertices which is adjacent to atleast one vertex in C and thus the vertices in C are independent.

The process goes in such a way, so that we get the IDN for  $3A(Q_n)$  as (i.e.,)

$$i(3A(Q_n)) = \left[\frac{n}{3}\right]$$

Theorem 3.3:

Let us take the graph  $4A(Q_n)$  with the path  $P_n$ , then  $i(4A(Q_n)) = \left\lfloor \frac{n}{3} \right\rfloor + N$  where N takes the values 0,1 twice alternatively in the series.

#### **Proof**:

Procedure for  $4A(Q_n)$ :

The  $4A(Q_n)$  graph is defined by adding two new vertex for every four edges of  $(v_{i-1}, v_i), (v_i, v_{i+1}), (v_{i+1}, v_{i+2})$  and  $(v_{i+2}, v_{i+3})$  alternatively.

Continue the process as in theorem 3.1, till  $A_n$ .

This graph is named as G and now we find the set C (ID set) from a graph  $4A(Q_n)$ , such that V-C has vertices which is adjacent to atleast one vertex in C and thus the vertices in C are independent.

The process goes in such a way, so that we get the IDN for  $4A(Q_n)$  as (i.e.,)  $i(4A(Q_n)) = \left|\frac{n}{4}\right| + N$  where N takes the values 0,1 twice alternatively in the series.

Theorem 3.4:

Let us take the graph  $5A(Q_n)$  with the path  $P_n$ , then  $i(5A(Q_n)) = \left|\frac{n}{2}\right|$ 

#### **Proof**:

Procedure for  $5A(Q_n)$ :

The  $5A(Q_n)$  is defined by adding two new vertex for every five edges of  $(v_{i-1}, v_i), (v_i, v_{i+1}), (v_{i+1}, v_{i+2}), (v_{i+2}, v_{i+3})$  and  $(v_{i+3}, v_{i+4})$  alternatively.

The rest of the procedure is carried out as in theorem 3.1, till  $A_n$ .

This graph is named as G and now we find the set C (ID set) from a graph  $5A(Q_n)$ , such that V-C has vertices which is adjacent to atleast one vertex in C and thus the vertices in C are independent.

The process goes in such a way, so that we get the IDN for  $5A(Q_n)$  as (i.e.,)

$$i(5A(Q_n)) = \left\lceil \frac{n}{3} \right\rceil$$

Section-4

#### IDN in

(i)  $2A(D(Q_n))$  (ii)  $3A(D(Q_n))$  (iii)  $4A(D(Q_n))$  (iv)  $5A(D(Q_n))$ 

Theorem 4.1:

Let us take the graph  $2A(D(Q_n))$  with the path  $P_n$  then  $i(2A(D(Q_n)) = \left\lfloor \frac{n}{3} \right\rfloor + N$  where N takes 0,1,2... twice in the series.

**Proof**:

Procedure for  $2A(D(Q_n))$ :

The  $2A(D(Q_n))$  graph is defined by adding two vertices above and below the common path for every two edges of  $v_{i-1}$ ,  $v_i$  and  $v_i$ ,  $v_{i+1}$  alternatively.

We label the root path of the vertices as  $v_1, v_2, ..., v_n$  thereby we add the vertices above the root path as  $a_1b_1, a_2b_2$  and below the root path as  $c_1d_1, c_2d_2$  to the corresponding edges  $v_1, v_2$  and  $v_2, v_3$  respectively.

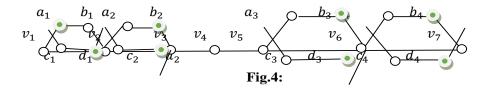
Leave the next two edges  $v_3$ ,  $v_4$  and  $v_4$ ,  $v_5$ .

Continue process till  $A_n$  as in section 3 theorem 3.1 (by adding the vertices above and below the common path).

This graph is named as G and now we find the set C (ID set) from a graph  $2A(D(Q_n))$ , such that V-C has vertices which is adjacent to atleast one vertex in C and thus the vertices in C are independent.

The process goes in such a way, so that we get the IDN for  $2A(D(Q_n))$  as (i.e.,)

$$i(2A(D(Q_n)) = \left|\frac{n}{3}\right| + N$$
 where N takes 0,1,2... twice in the series



Theorem 4.2:

Let us take the graph  $3A(D(Q_n))$  with the path  $P_n$  then  $i(3A(D(Q_n)) = \left\lfloor \frac{n}{3} \right\rfloor + N$  where N takes 0,1,2... twice in the series.

# **Proof**:

Procedure for  $3A(D(Q_n))$ :

The  $3A(D(Q_n))$  graph is defined by adding two new vertices above and below the common path for every three edges of  $(v_{i-1}, v_i), (v_i, v_{i+1})$  and  $(v_{i+1}, v_{i+2})$  alternatively.

Continue the process till  $A_n$  as in section 3 theorem 3.1 (by adding the vertices above and below the common path).

This graph is named as G and now we find the set C (ID set) from a graph  $3A(D(Q_n))$ , such that V-C has vertices which is adjacent to atleast one vertex in C and thus the vertices in C are independent.

The process goes in such a way, so that we get the IDN for  $3A(D(Q_n))$  as (i.e.,)

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$$i(3A(D(Q_n)) = \left|\frac{n}{3}\right| + N$$
 where N takes 0,1,2... twice in the series.

Theorem 4.3:

Let us take the graph  $4A(D(Q_n))$  with the path  $P_n$  then  $i(4A(D(Q_n)) = \left\lfloor \frac{n}{3} \right\rfloor + N$  where N takes 1,2,3... twice in the series.

#### **Proof**:

Procedure for  $4A(D(Q_n))$ :

The  $4A(D(Q_n))$  graph is defined by adding two new vertex above and below the common path for every four edges of  $(v_{i-1}, v_i), (v_i, v_{i+1}), (v_{i+1}, v_{i+2})$  and  $(v_{i+2}, v_{i+3})$  alternatively.

Continue the process till  $A_n$  as in section 3 theorem 3.1 (by adding the vertices above and below the common path).

This graph is named as G and now we find the set C (ID set) from a graph  $3A(D(Q_n))$ , such that V-C has vertices which is adjacent to atleast one vertex in C and thus the vertices in C are independent.

The process goes in such a way, so that we get the IDN for  $4A(D(Q_n))$  as (i.e.,)

 $i(4A(D(Q_n)) = \left\lfloor \frac{n}{3} \right\rfloor + N$  where N takes 1,2,3... twice in the series.

Theorem 4.4:

Let us take the graph  $5A(D(Q_n))$  with the path  $P_n$  then  $i(5A(D(Q_n)) = \left\lfloor \frac{n}{3} \right\rfloor + N$  where N takes 1,3,5,7... twice in the series.

#### **Proof**:

Procedure for  $5A(D(Q_n))$ :

The  $5A(D(Q_n))$  graph is defined by adding two new vertex above and below the common path for every five edges of  $(v_{i-1}, v_i), (v_i, v_{i+1}), (v_{i+1}, v_{i+2}), (v_{i+2}, v_{i+3})$  and  $(v_{i+3}, v_{i+4})$  alternatively.

Continue the process till  $A_n$  as in section 3 theorem 3.1 (by adding the vertices above and below the common path).

Now this graph is named as G and now we find the set C (ID set) from a graph  $3A(D(Q_n))$ , such that V-C has vertices which is adjacent to atleast one vertex in C and thus the vertices in C are independent.

The process goes in such a way, so that we get the IDN for  $5A(D(Q_n))$  as (i.e.,)

 $i(5A(D(Q_n)) = \left\lfloor \frac{n}{3} \right\rfloor + N$  where N takes 1,3,5,7... twice in the series.

#### 2. CONCLUSION

In our previous works we have found IDN for different types of networks. In this paper we found IDN for some special types of snake graphs. Further, this work can be extended for n-number of types of alternate snake graphs, which we restricted in our research from 2-5 alternate snake graphs, therefore the remaining networks are left to the readers as an open question.

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